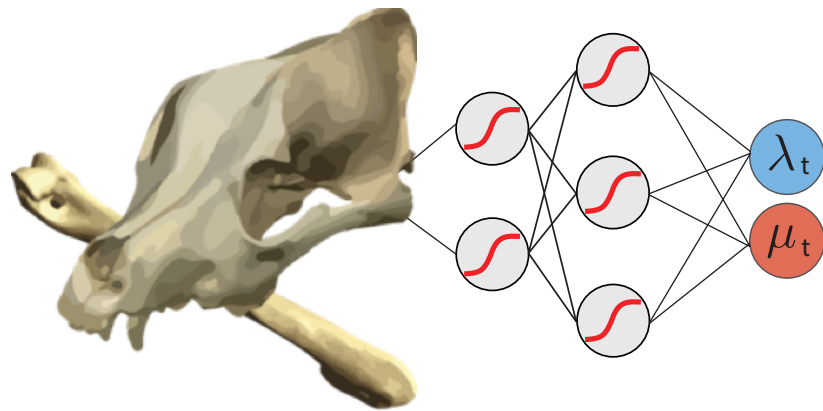


Bayesian and deep learning for macroevolutionary analyses



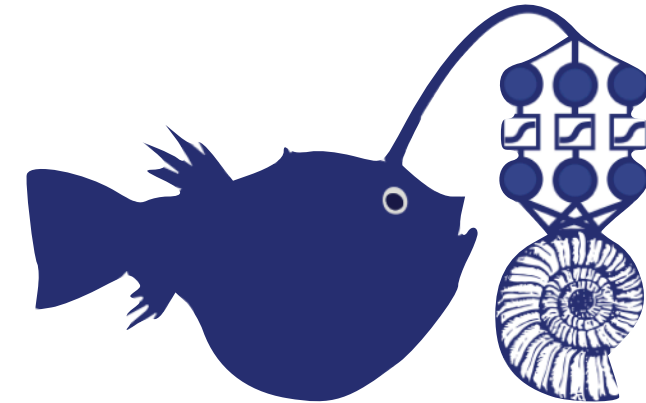
Gemini's take on our workshop

Learning objectives



PyRate and the BDNN model

Estimating trait and time dependent speciation and extinction rates from fossil occurrence data



DeepDive

Estimating diversity trajectories through time using deep learning and mechanistic simulations

(And more!)



PyRate

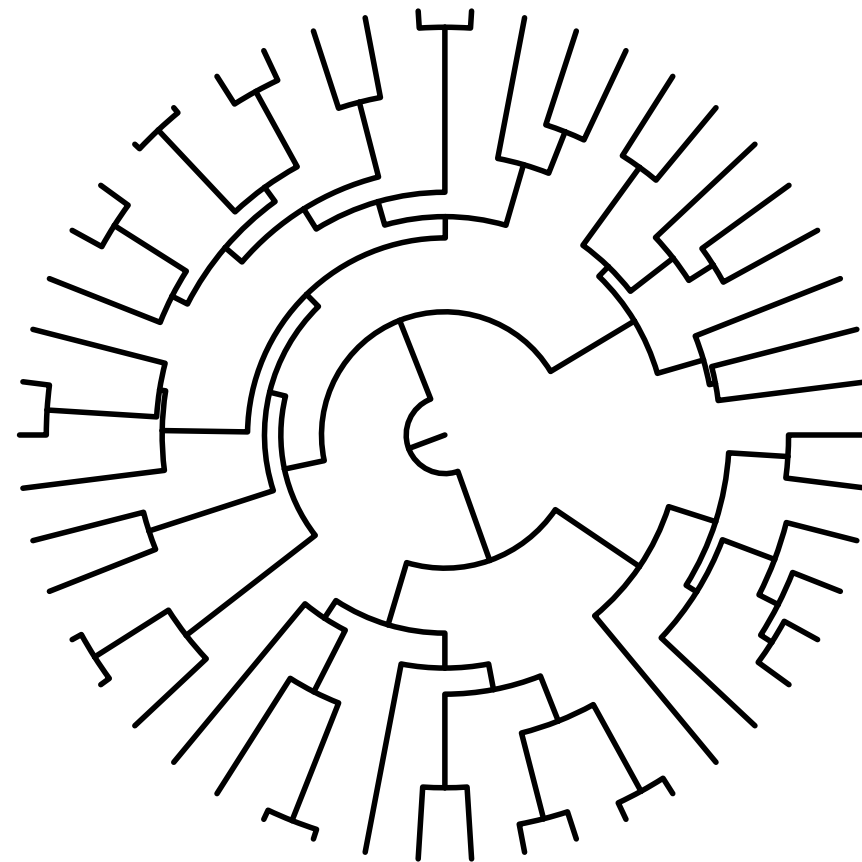
Bayesian estimation of
macroevolutionary rates from
fossil occurrence data

Estimation of macroevolutionary rates from the fossil record





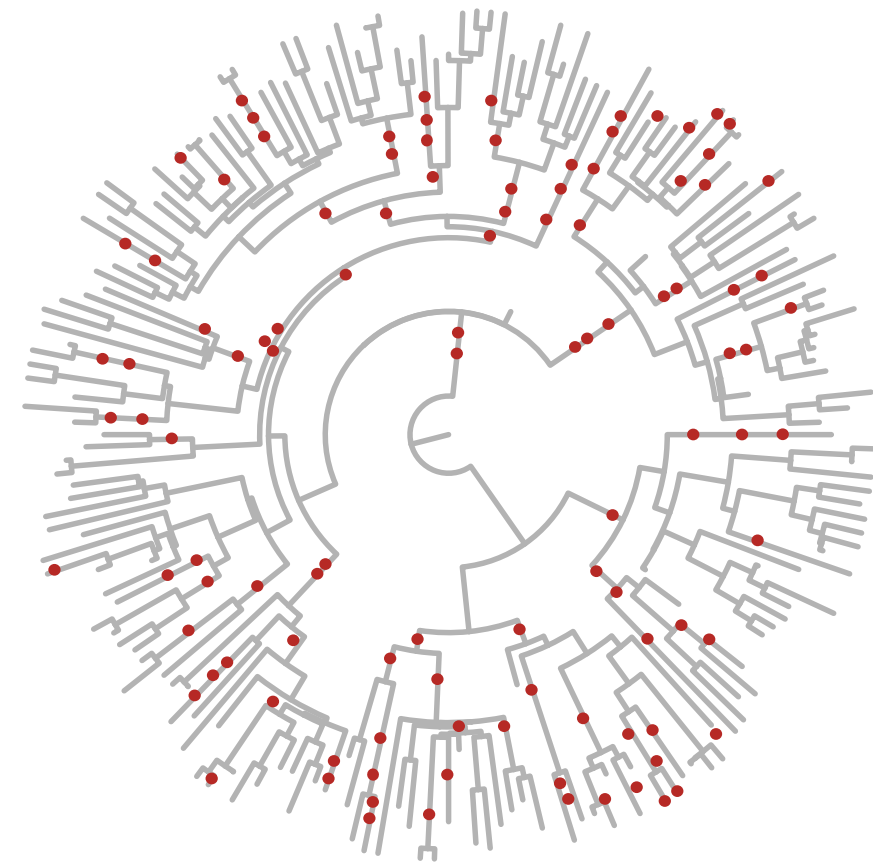
Complete evolutionary history of a clade



Reconstructed phylogeny of the extant taxa



Phylogenetic comparative methods



Fossil record

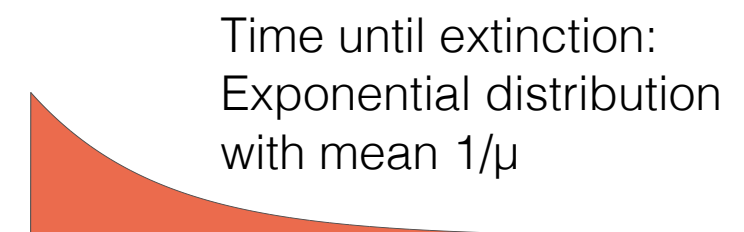
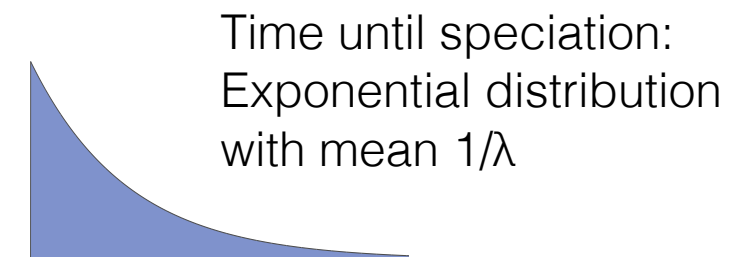
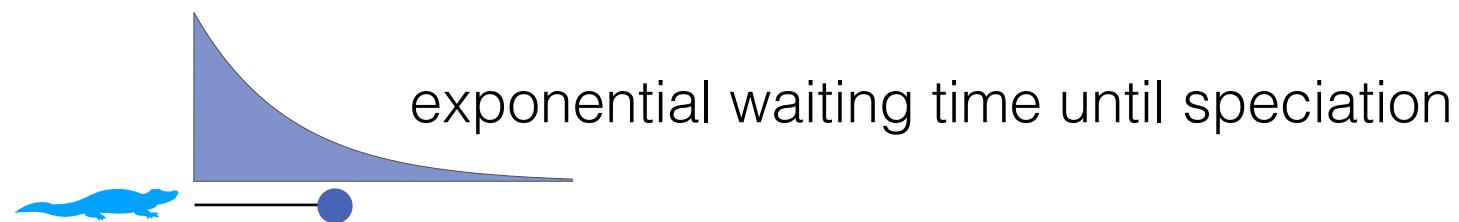


“Stratigraphic approaches”

Species diversification as a birth-death stochastic process

λ : expected number of speciation events in 1 My per-lineage

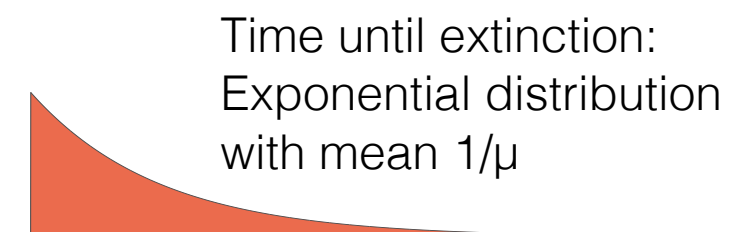
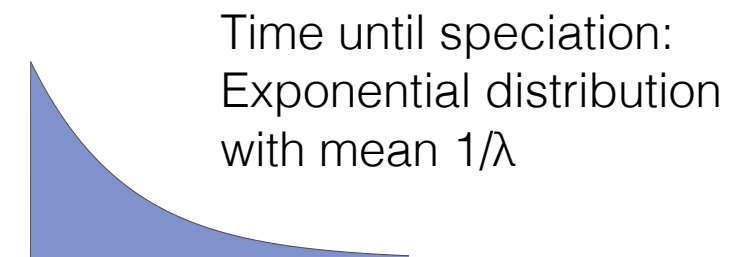
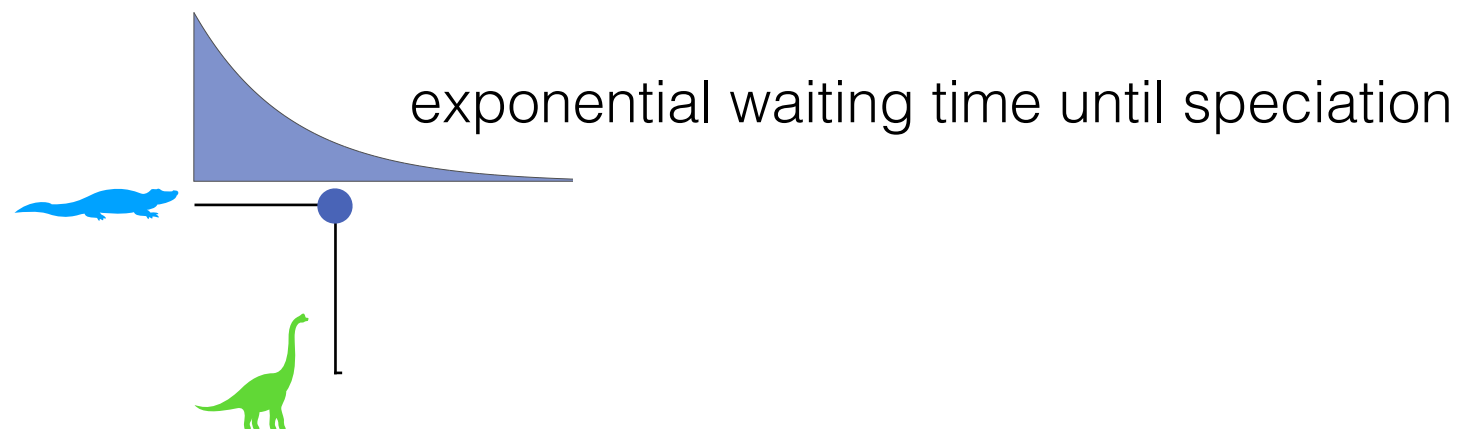
μ : expected number of extinction events in 1 My per-lineage



Species diversification as a birth-death stochastic process

λ : expected number of speciation events in 1 My per-lineage

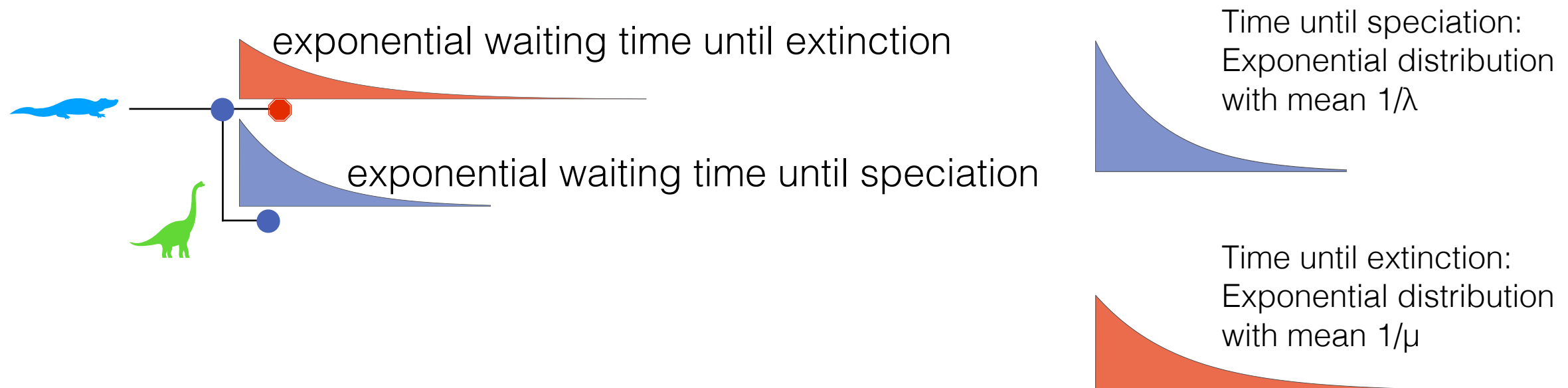
μ : expected number of extinction events in 1 My per-lineage



Species diversification as a birth-death stochastic process

λ : expected number of speciation events in 1 My per-lineage

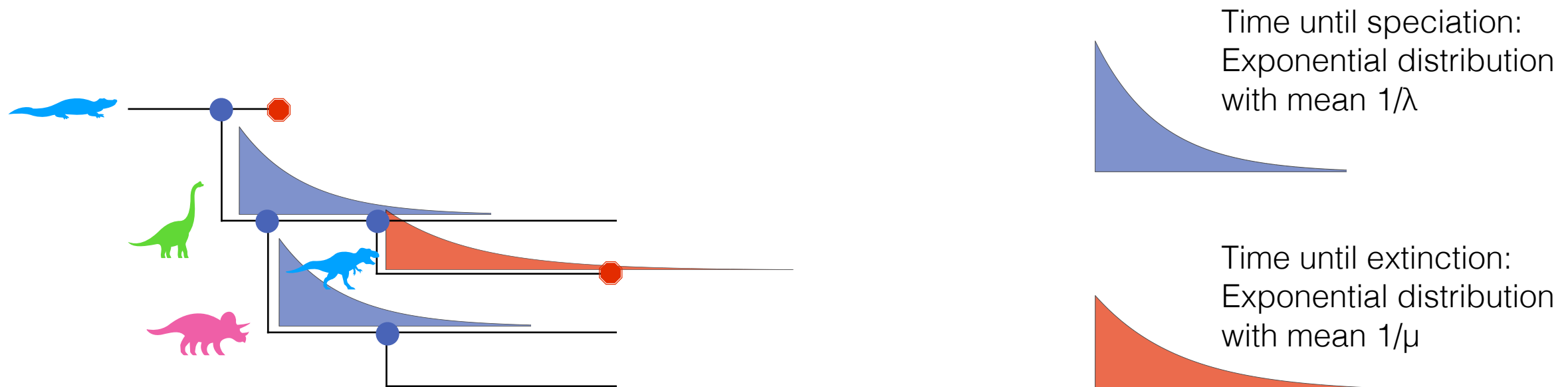
μ : expected number of extinction events in 1 My per-lineage



Species diversification as a birth-death stochastic process

λ : expected number of speciation events in 1 My per-lineage

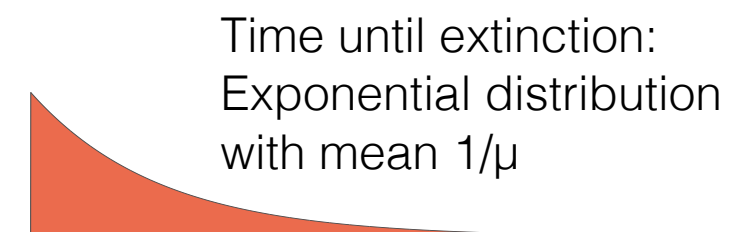
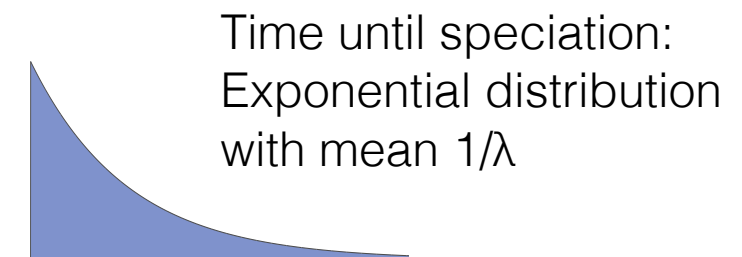
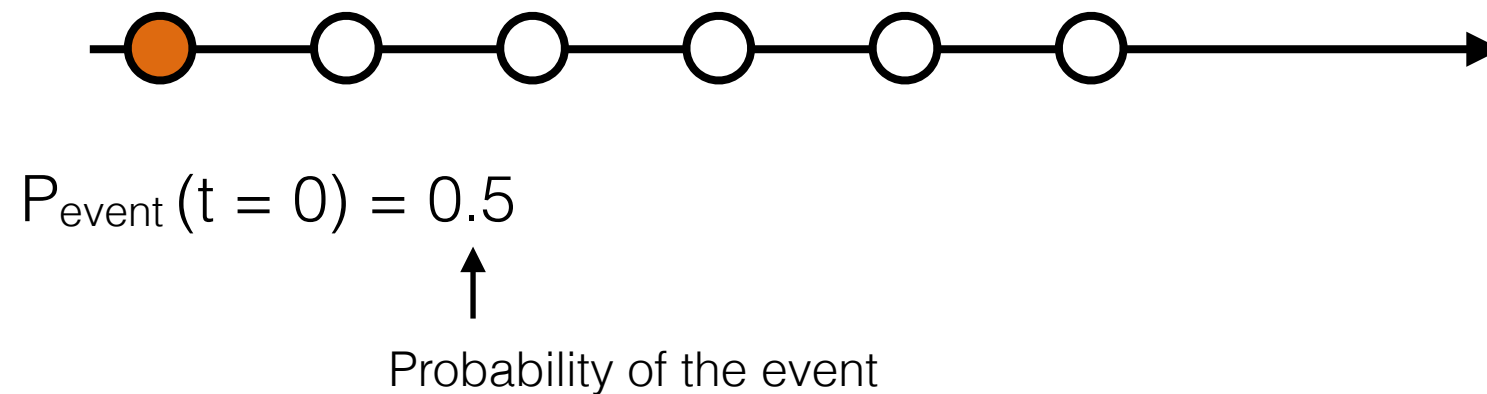
μ : expected number of extinction events in 1 My per-lineage



Species diversification as a birth-death stochastic process

Why an exponential waiting time?

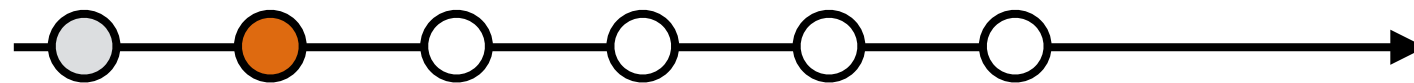
Expected pattern from a constant rate random process



Species diversification as a birth-death stochastic process

Why an exponential waiting time?

Expected pattern from a constant rate random process



$$P_{\text{event}}(t = 2) = 0.5 \times (1 - 0.5)^{t-1} = 0.25$$

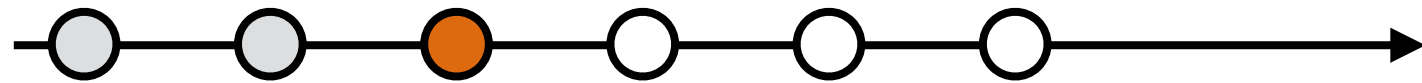
↑
Probability of the event

↑
Probability that it didn't
occur before time t

Species diversification as a birth-death stochastic process

Why an exponential waiting time?

Expected pattern from a constant rate random process



$$P_{\text{event}}(t = 3) = 0.5 \times (1 - 0.5)^{t-1} = 0.125$$

↑
Probability of the event

↑
Probability that it didn't
occur before time t

Species diversification as a birth-death stochastic process

Why an exponential waiting time?

Expected pattern from a constant rate random process



$$P_{\text{event}}(t = 4) = 0.5 \times (1 - 0.5)^{t-1} = 0.063$$

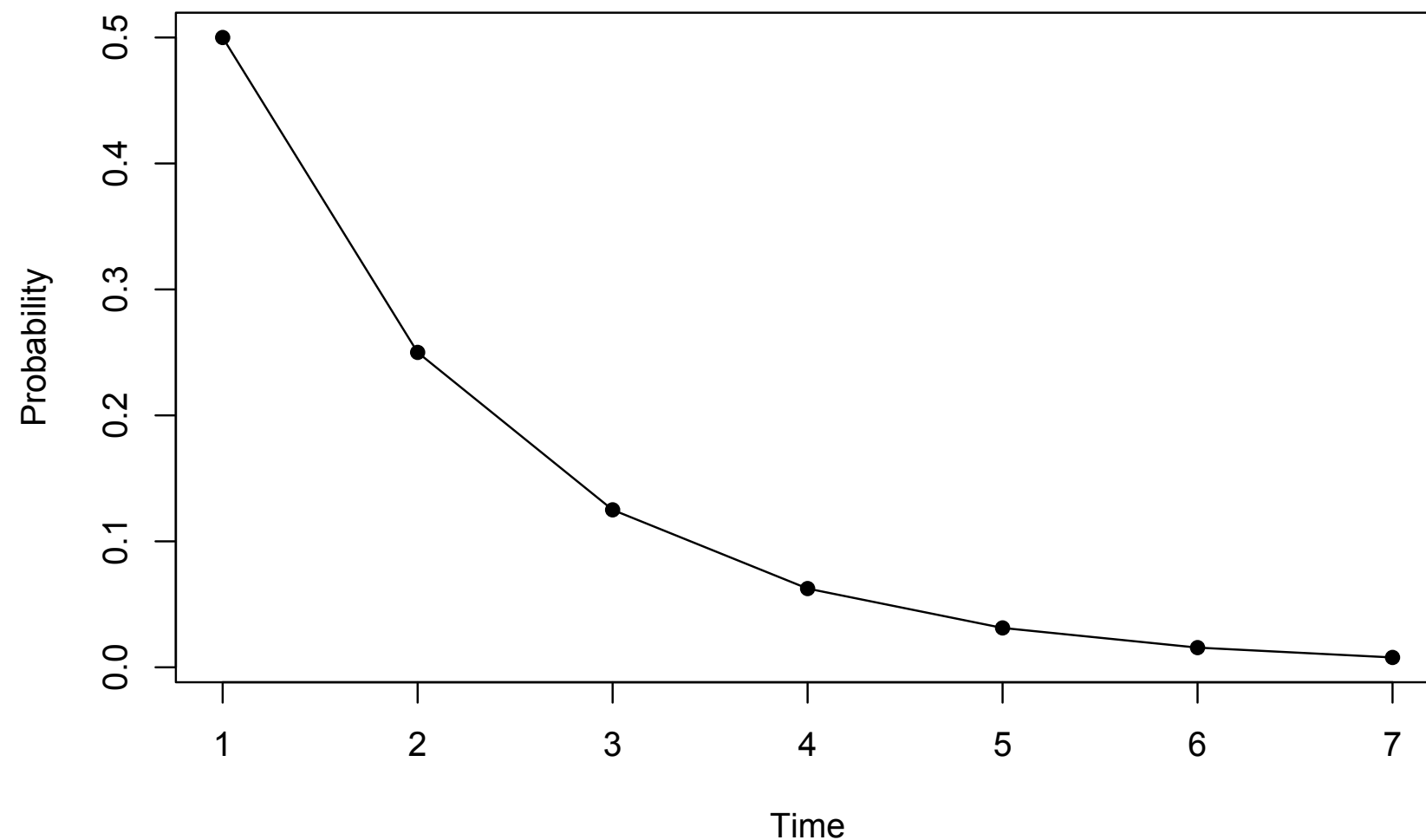
↑
Probability of the event

↑
Probability that it didn't
occur before time t

Species diversification as a birth-death stochastic process

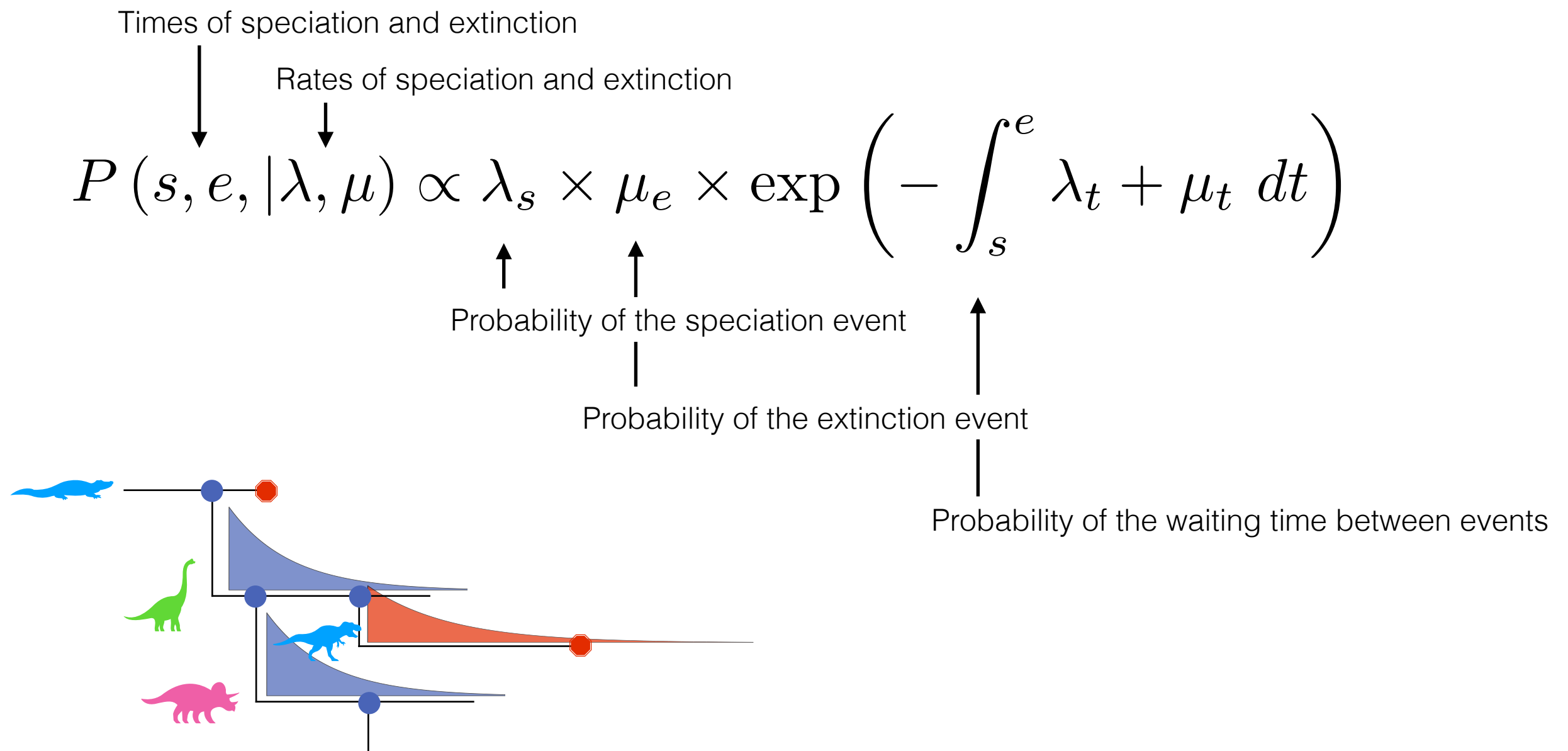
Why an exponential waiting time?

Expected pattern from a constant rate random process



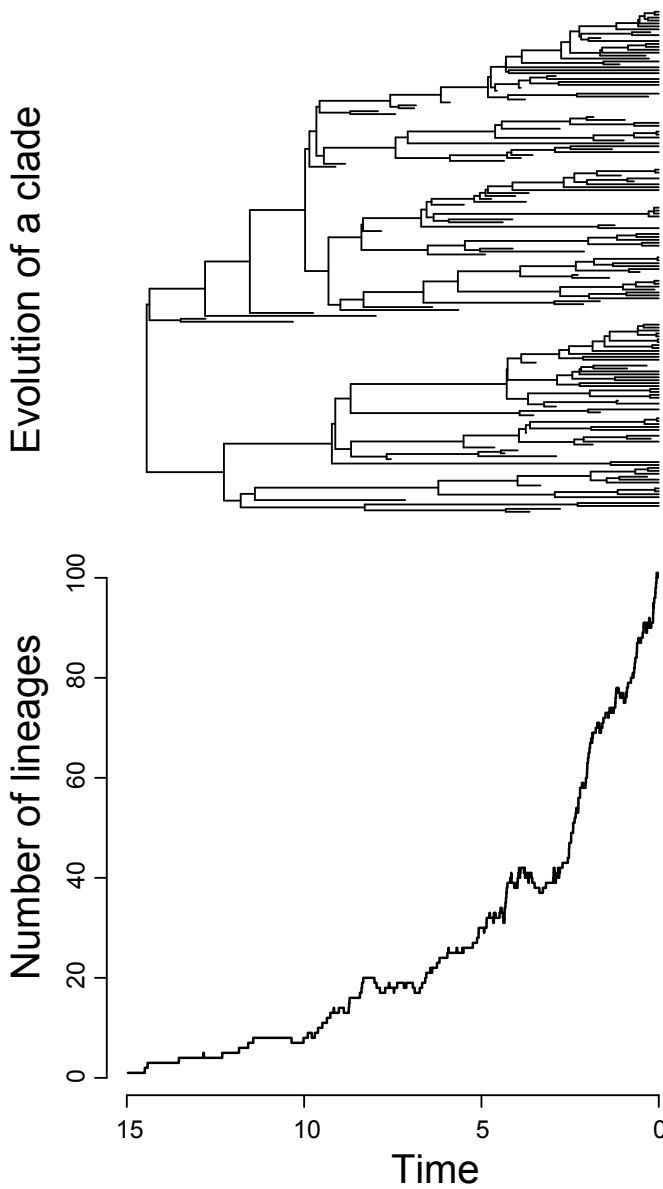
Species diversification as a birth-death stochastic process

Likelihood of a birth-death process

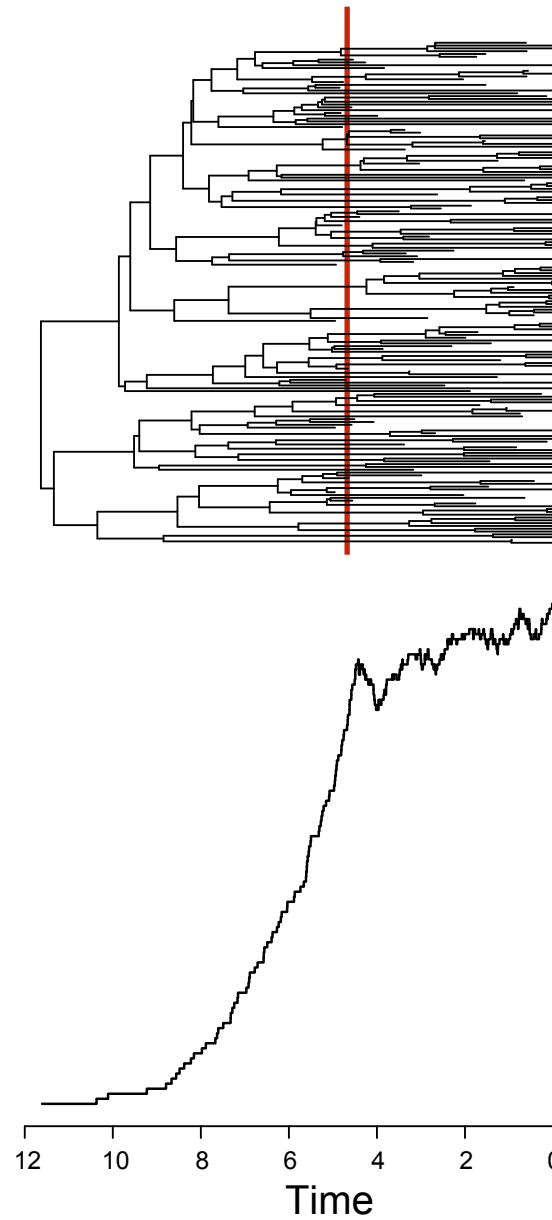


Understanding the process of diversification

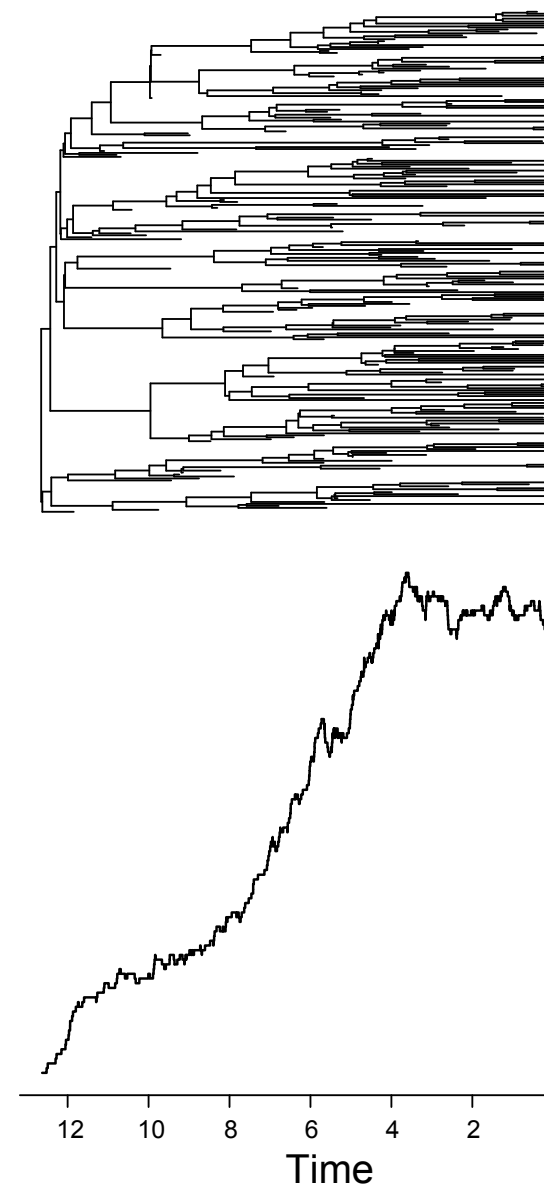
Constant speciation and extinction rate



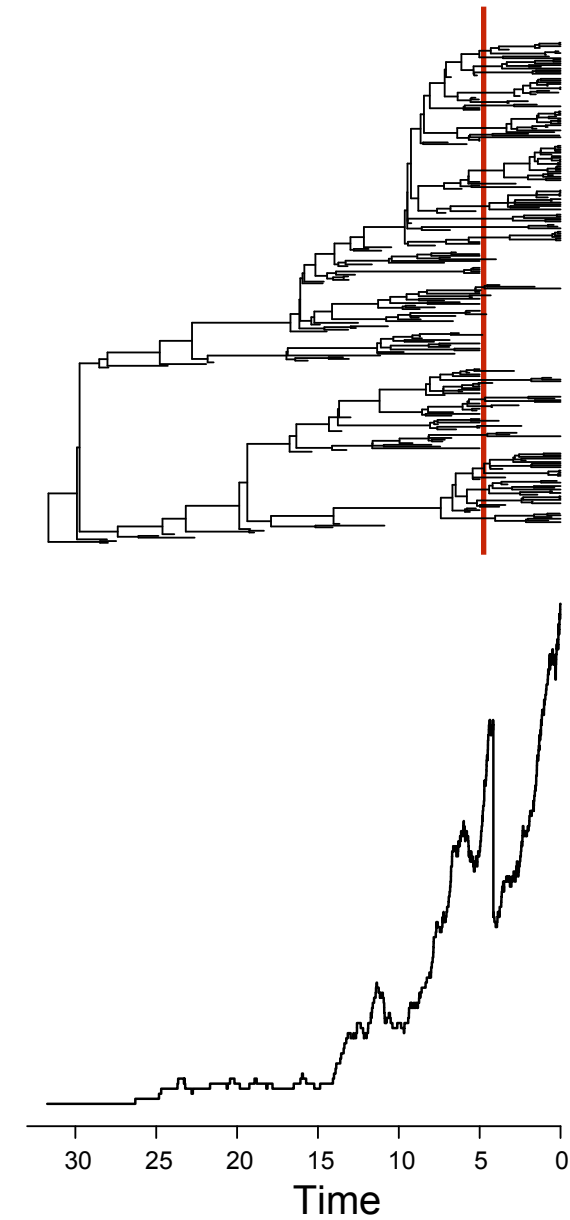
Rate shifts



Diversity dependent speciation rate

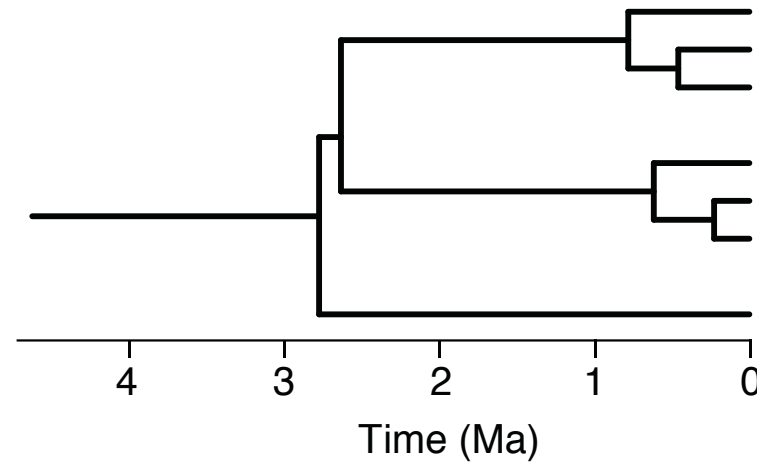


Mass extinction

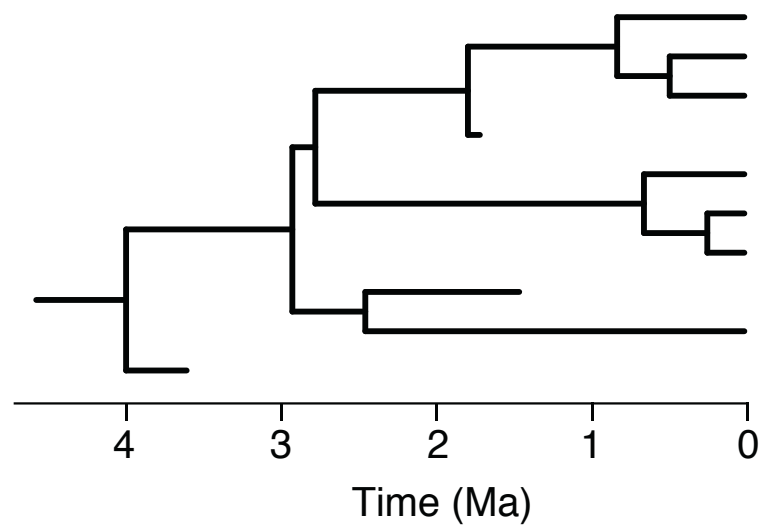


Methods to infer speciation and extinction rates

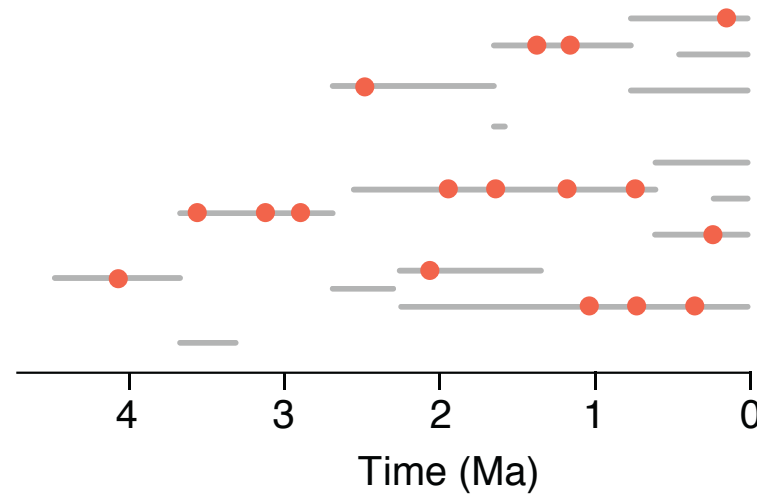
Phylogeny of extant species



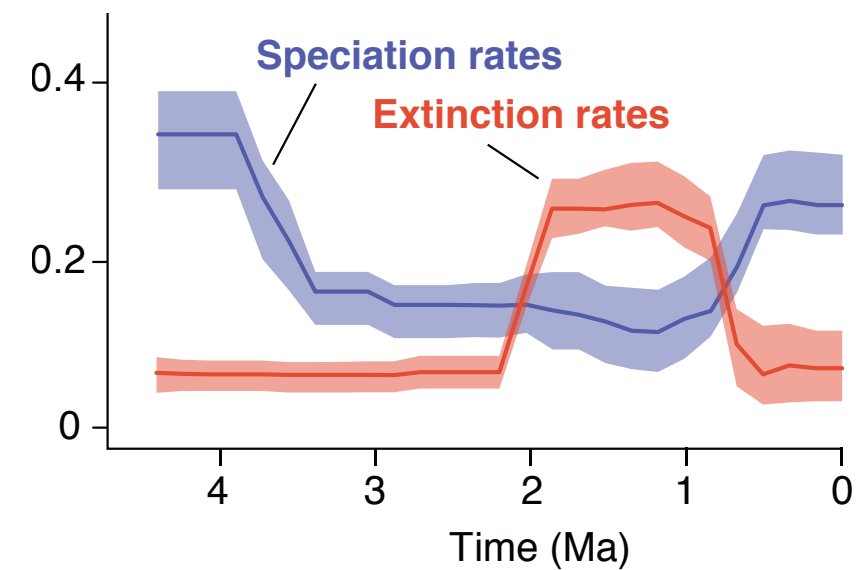
Complete evolutionary history



Fossil record



Diversification dynamics



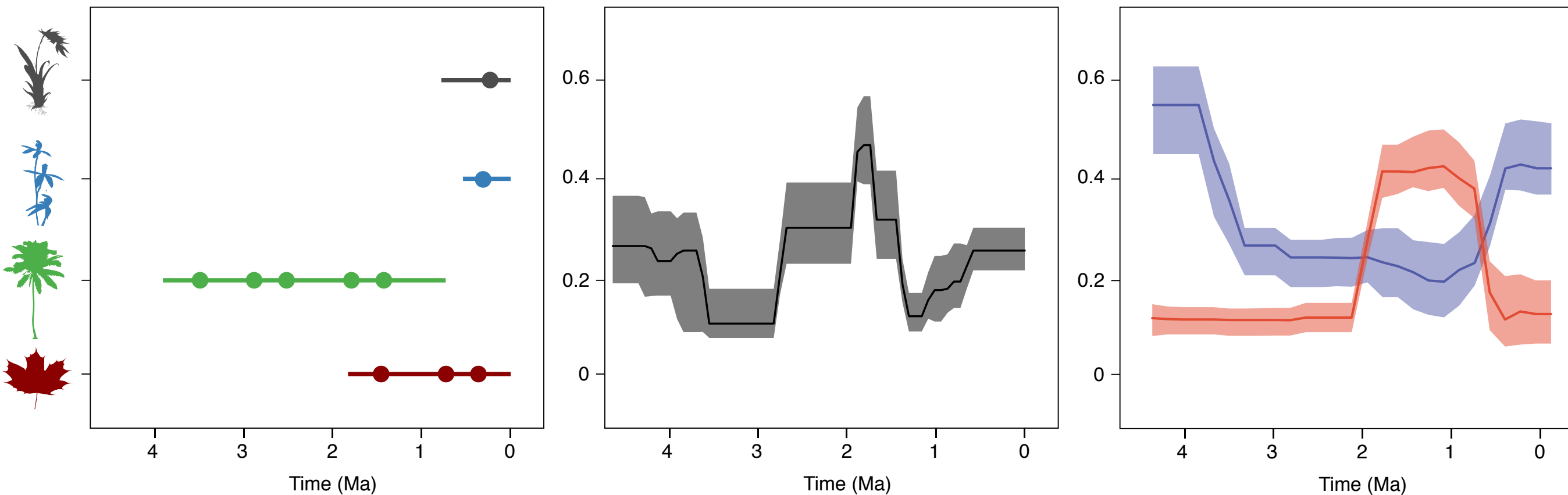
Bayesian inference of macroevolutionary rates using fossil occurrences

$$\underbrace{P(q, \mathbf{s}, \mathbf{e}, \lambda, \mu | X)}_{\text{posterior}} \propto \underbrace{P(X | q, \mathbf{s}, \mathbf{e})}_{\text{likelihood}} \times \underbrace{P(\mathbf{s}, \mathbf{e} | \lambda, \mu)}_{\text{BD prior}} \times \underbrace{P(q)P(\lambda, \mu)}_{\text{other (hyper-)priors}}$$

Taxa duration

Preservation rates

Speciation & **extinction** rates



PYRATE

<https://github.com/dsilvestro/PyRate>

Silvestro et al. 2014 Syst Biol, MEE

$$P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q)P(\lambda, \mu)$$

POSTERIOR LIKELIHOOD PRIOR HYPERPRIORS

↑
Probability of:
1. times of speciation/extinction (s, e)
2. preservation rate (q)
3. speciation/extinction rates (λ, μ)

A hierarchical probabilistic framework

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times \underbrace{P(s, e | \lambda, \mu)}_{\text{PRIOR}} \times \underbrace{P(q)P(\lambda, \mu)}_{\text{HYPERPRIORS}}$$

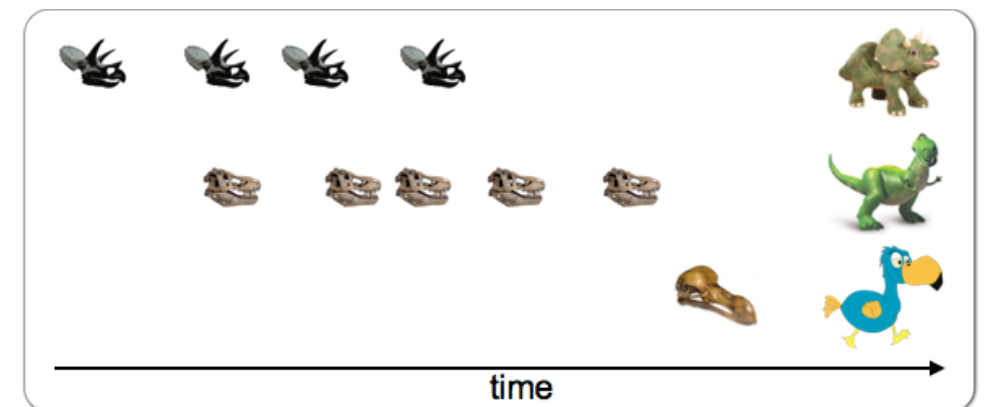
POSTERIOR

Probability of the data given speciation and extinction times, preservation rate

Probability of:

1. times of speciation/extinction (s, e)
2. preservation rate (q)
3. speciation/extinction rates (λ, μ)

$x =$



A hierarchical probabilistic framework

$$P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

POSTERIOR LIKELIHOOD PRIOR HYPERPRIORS

Prior probability of the speciation and extinction times (Birth-Death process)

The diagram shows the equation $P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$. Below the equation, the terms are labeled: POSTERIOR for the left side, LIKELIHOOD for $P(x | s, e, q)$, PRIOR for $P(s, e | \lambda, \mu)$, and HYPERPRIORS for $P(q) P(\lambda, \mu)$. The LIKELIHOOD term is highlighted with an orange box, and an arrow points from it to the text 'Prior probability of the speciation and extinction times (Birth-Death process)'. The PRIOR term is highlighted with a blue box.

A hierarchical probabilistic framework

$$P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q)P(\lambda, \mu)$$

POSTERIOR LIKELIHOOD PRIOR HYPERPRIORS

Prior distributions for rate parameters

The diagram illustrates a hierarchical probabilistic framework through the equation $P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q)P(\lambda, \mu)$. The equation is broken down into four components: POSTERIOR, LIKELIHOOD, PRIOR, and HYPERPRIORS. The LIKELIHOOD term $P(x | s, e, q)$ is highlighted with an orange box around q . The PRIOR term $P(s, e | \lambda, \mu)$ is highlighted with a blue box around λ, μ . The HYPERPRIORS term $P(q)P(\lambda, \mu)$ is highlighted with a purple box. Two arrows originate from the highlighted q and λ, μ terms and point towards the text 'Prior distributions for rate parameters'.

Bayesian inference of macroevolutionary rates using fossil occurrences

$$\underbrace{P(q, \mathbf{s}, \mathbf{e}, \lambda, \mu | X)}_{\text{posterior}} \propto \underbrace{P(X | q, \mathbf{s}, \mathbf{e})}_{\text{likelihood}} \times \underbrace{P(\mathbf{s}, \mathbf{e} | \lambda, \mu)}_{\text{birth-death prior}} \times \underbrace{P(q)P(\lambda, \mu)}_{\text{other (hyper)priors}}$$

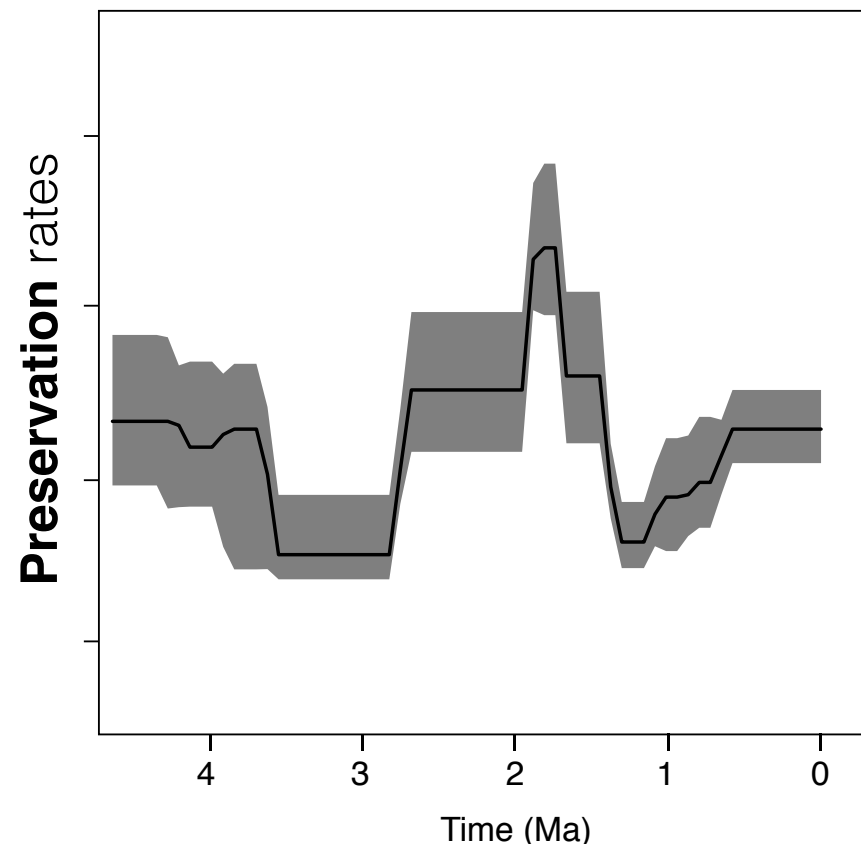
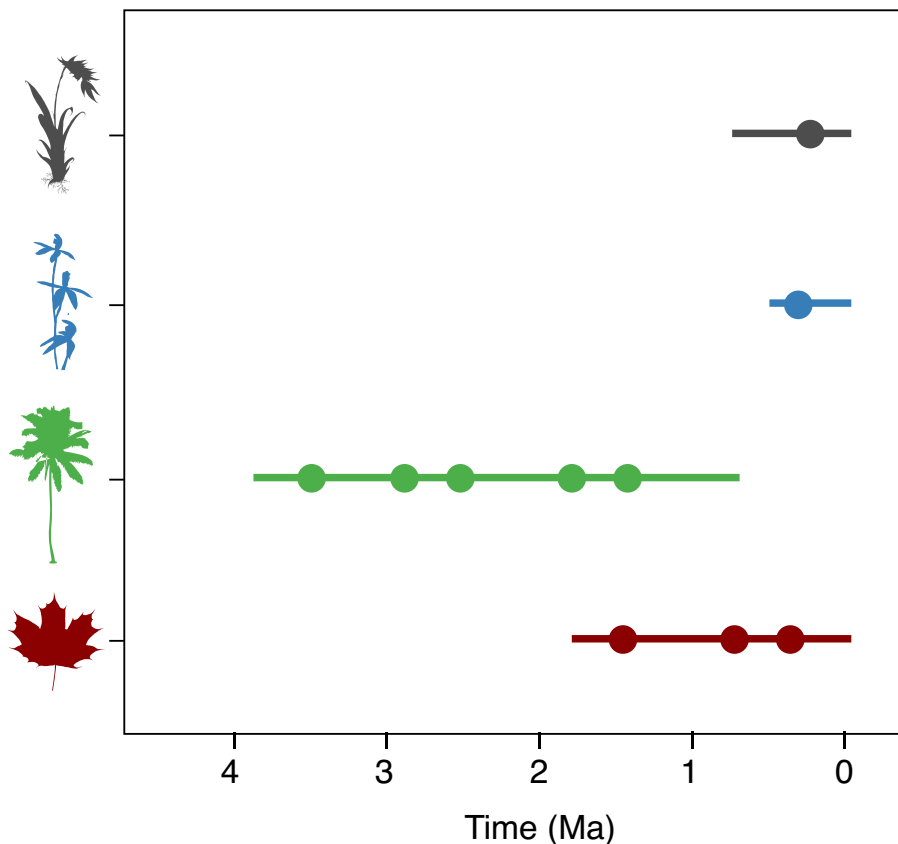
Metropolis-Hastings
MCMC

Reversible-jump
MCMC

Sampled directly from
conjugate posterior

Species duration

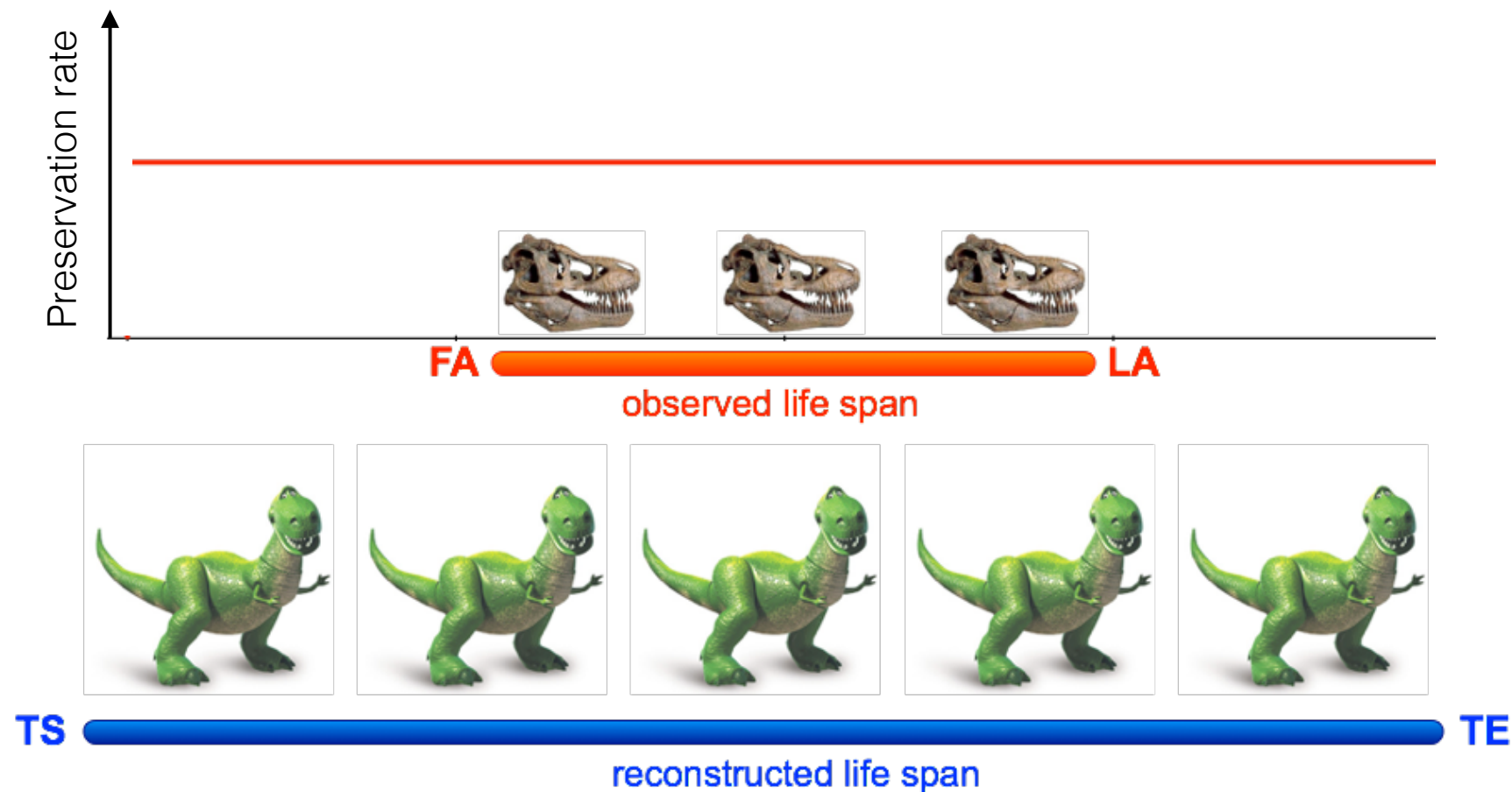
Poisson process



Estimated preservation rates and times of speciation and extinction

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

Homogeneous Poisson process (HPP)

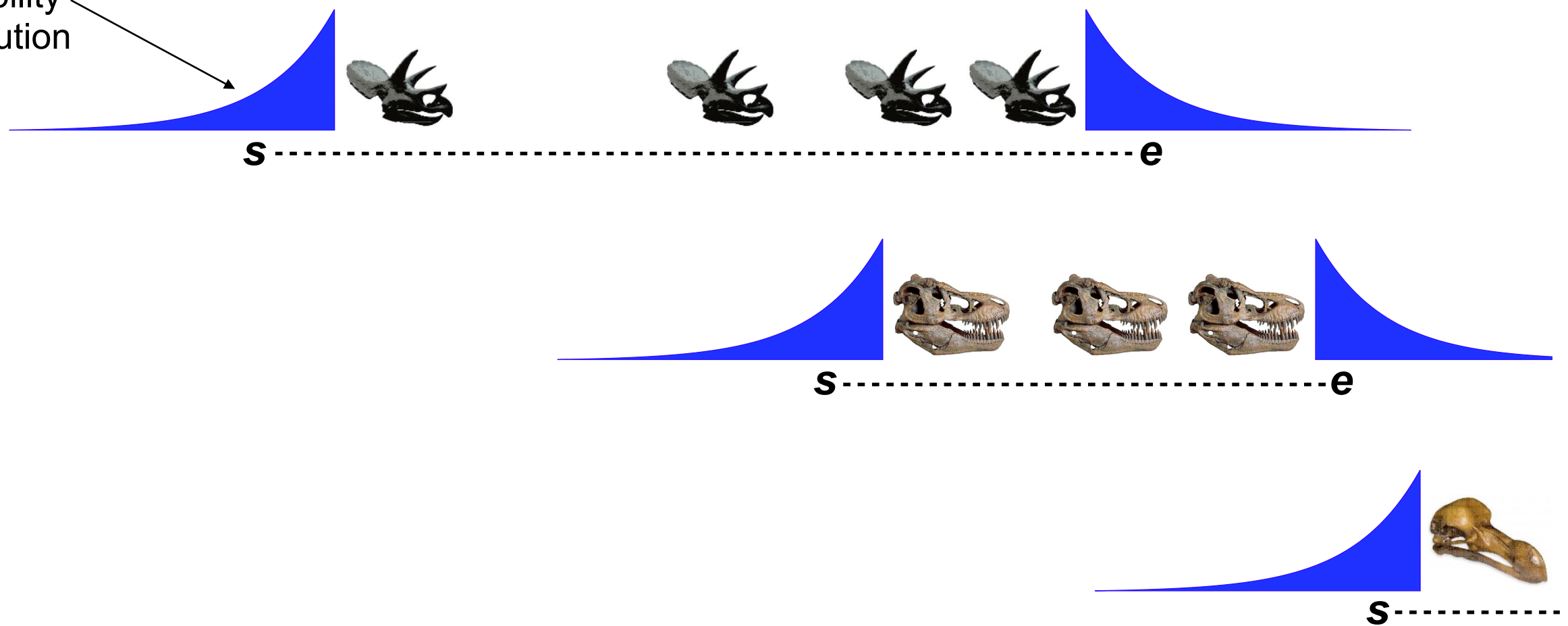


Estimated preservation rates and times of speciation and extinction

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

Homogeneous Poisson process (HPP)

Posterior probability distribution

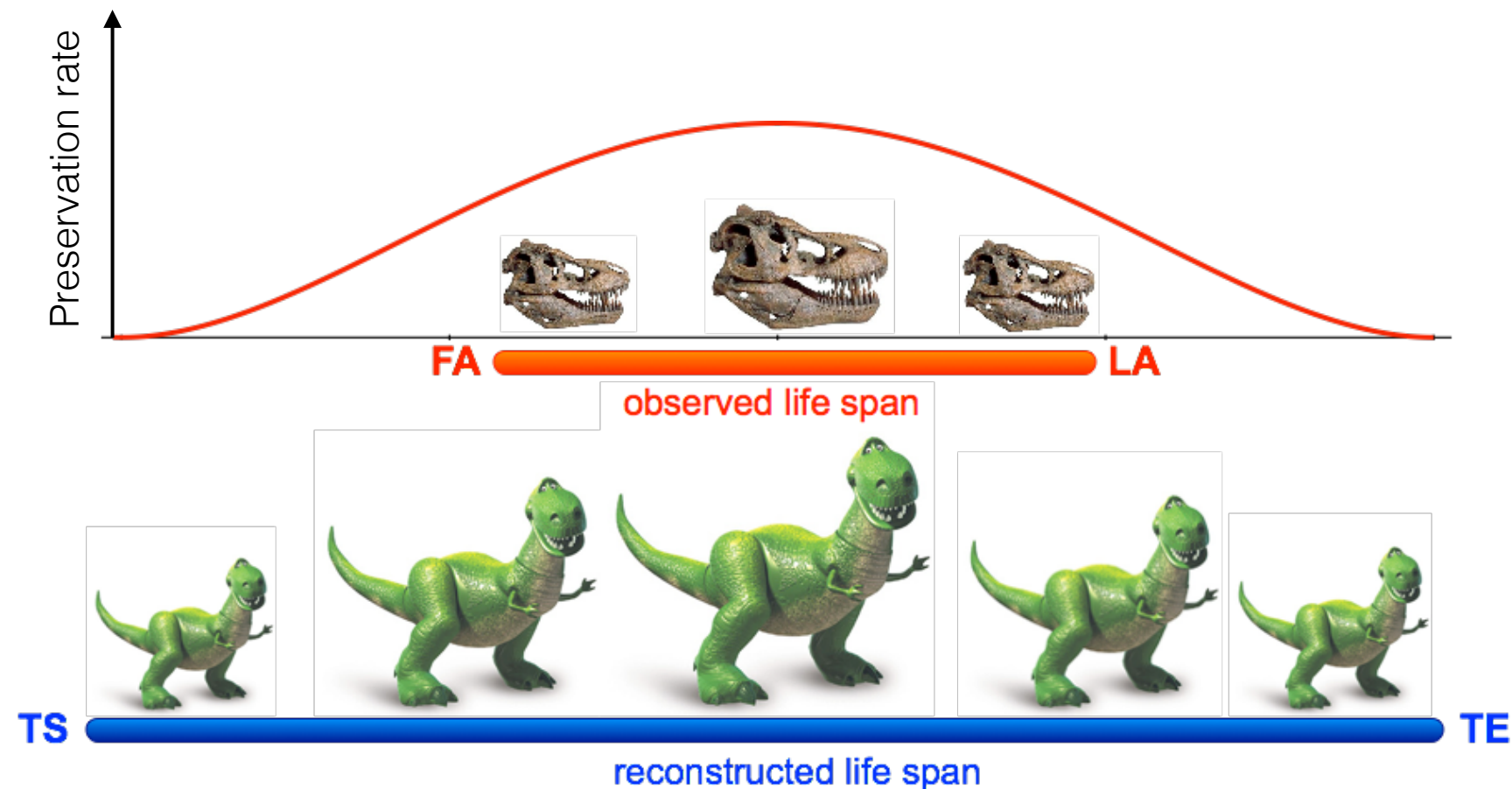


Constant preservation rate

Estimated preservation rates and times of speciation and extinction

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

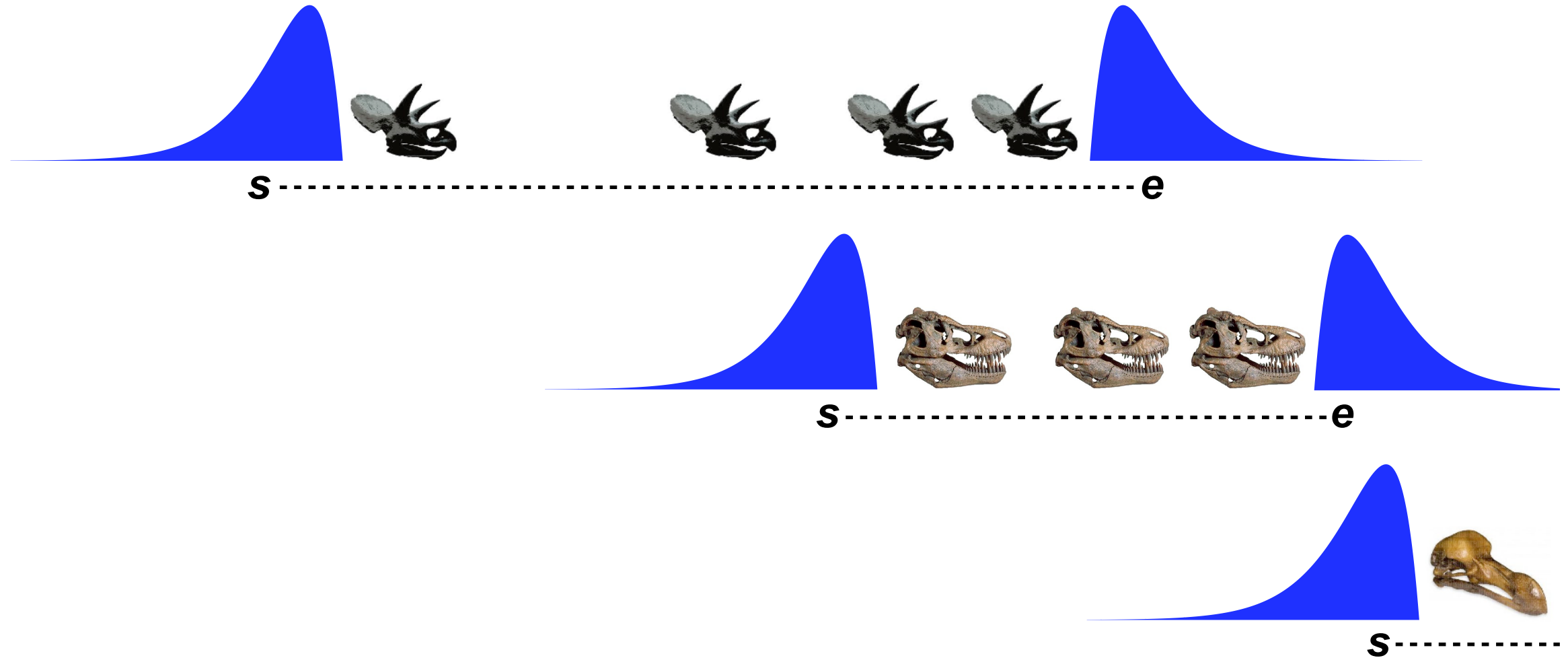
Non-homogeneous Poisson process (NHPP)



Estimated preservation rates and times of speciation and extinction

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

Non-homogeneous Poisson process (NHPP)

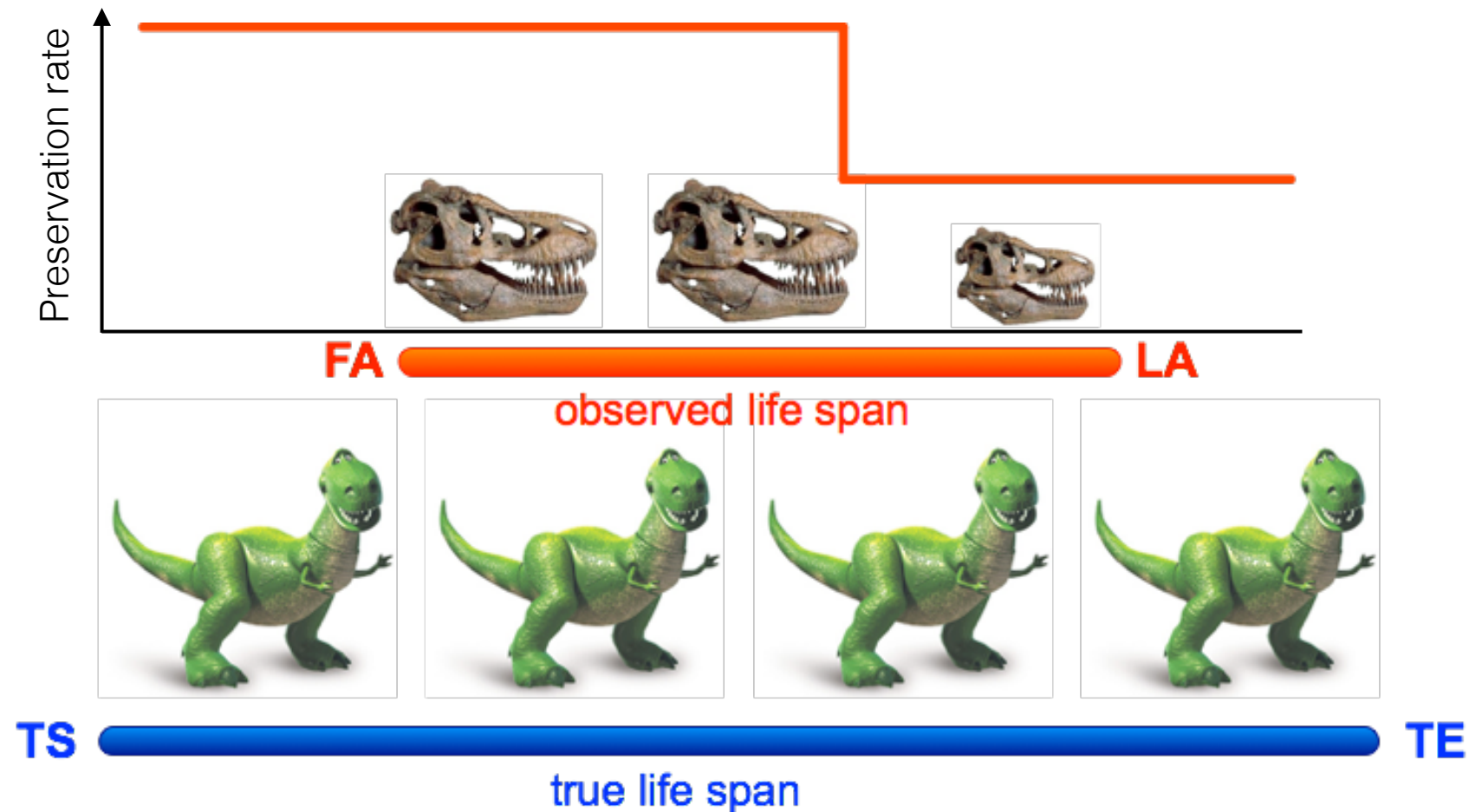


Constant mean preservation rate

Estimated preservation rates and times of speciation and extinction

$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

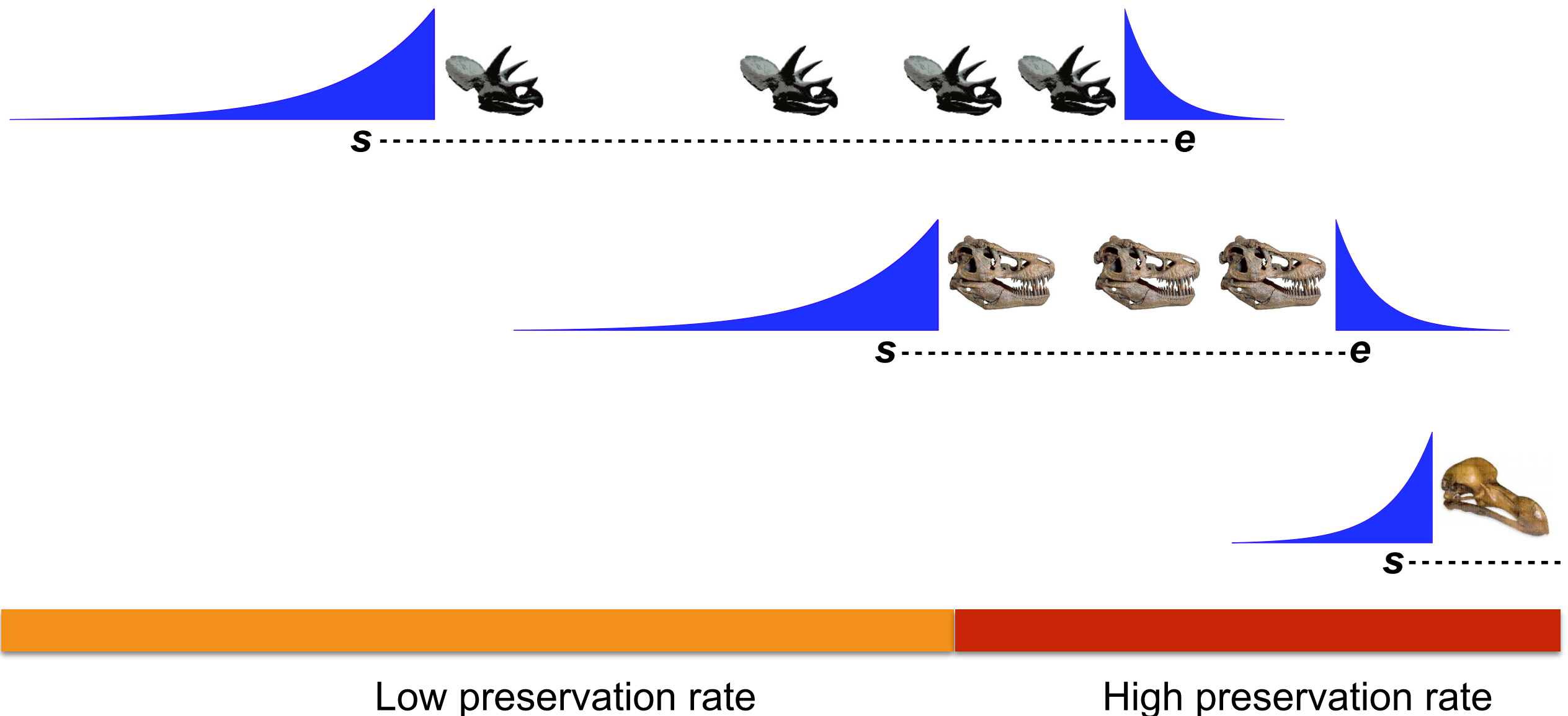
Time-variable Poisson process (TPP)



Estimated preservation rates and times of speciation and extinction

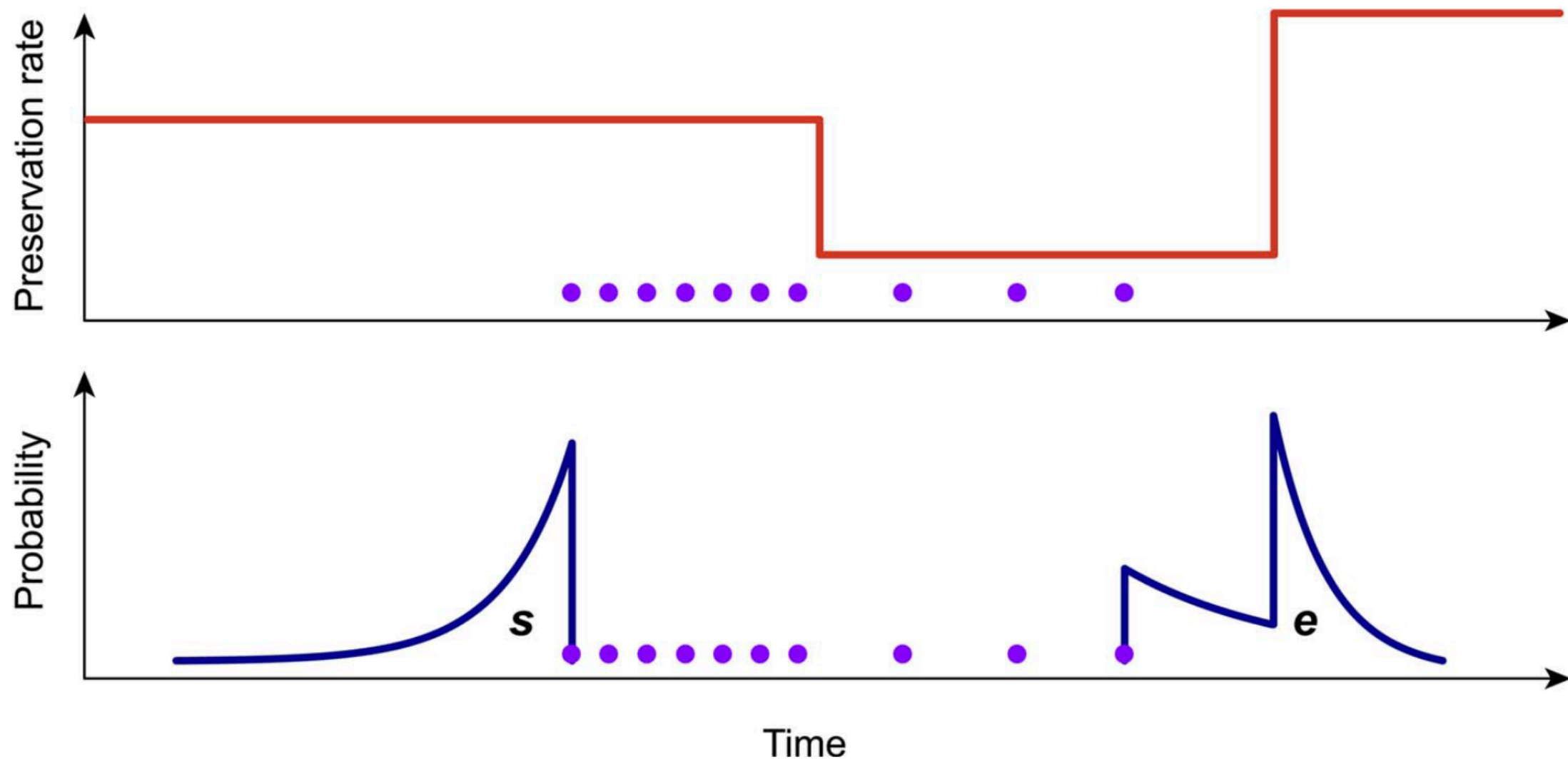
$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

Time-variable Poisson process (TPP)



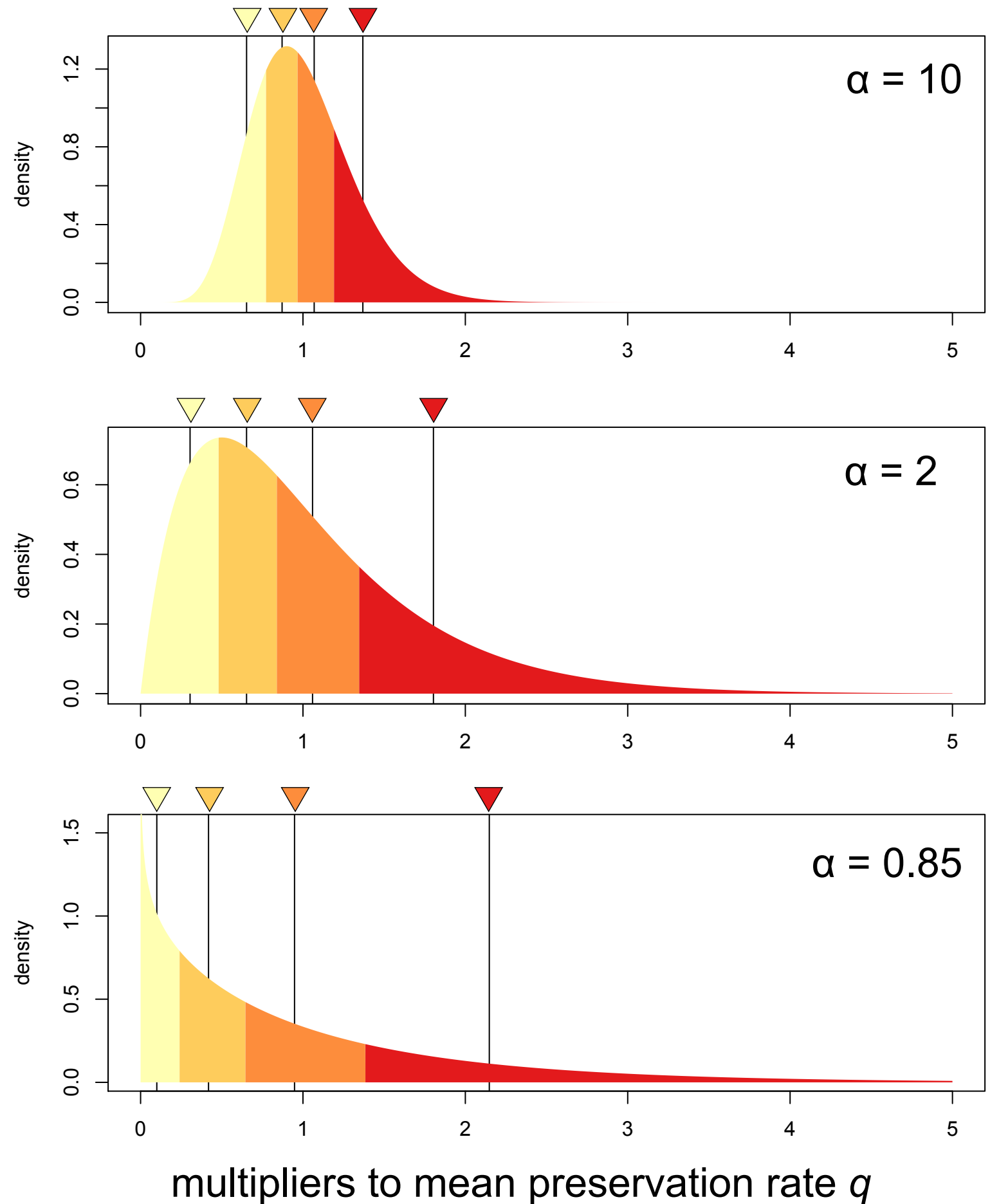
$$P(s, e, q, \lambda, \mu | x) \propto \underbrace{P(x | s, e, q)}_{\text{LIKELIHOOD}} \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

Time-variable Poisson process (TPP)

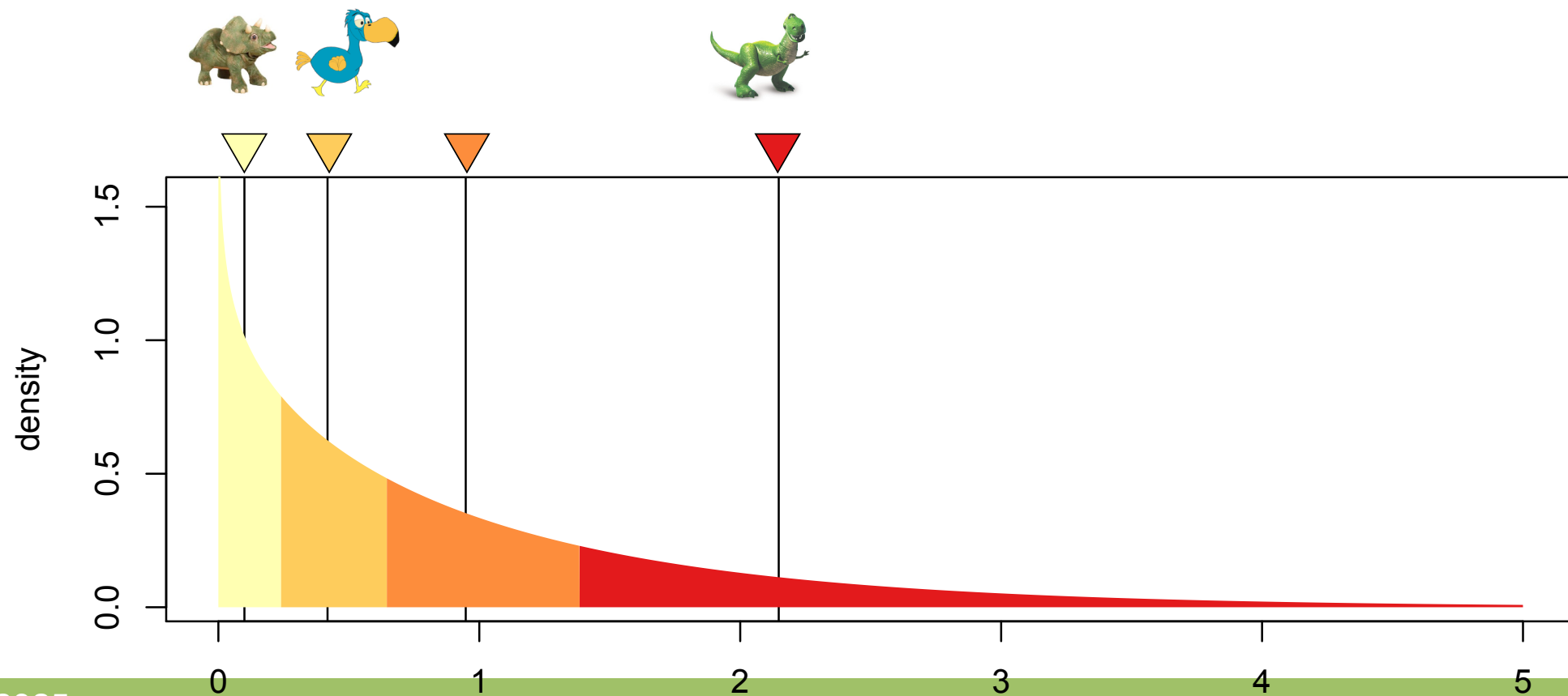
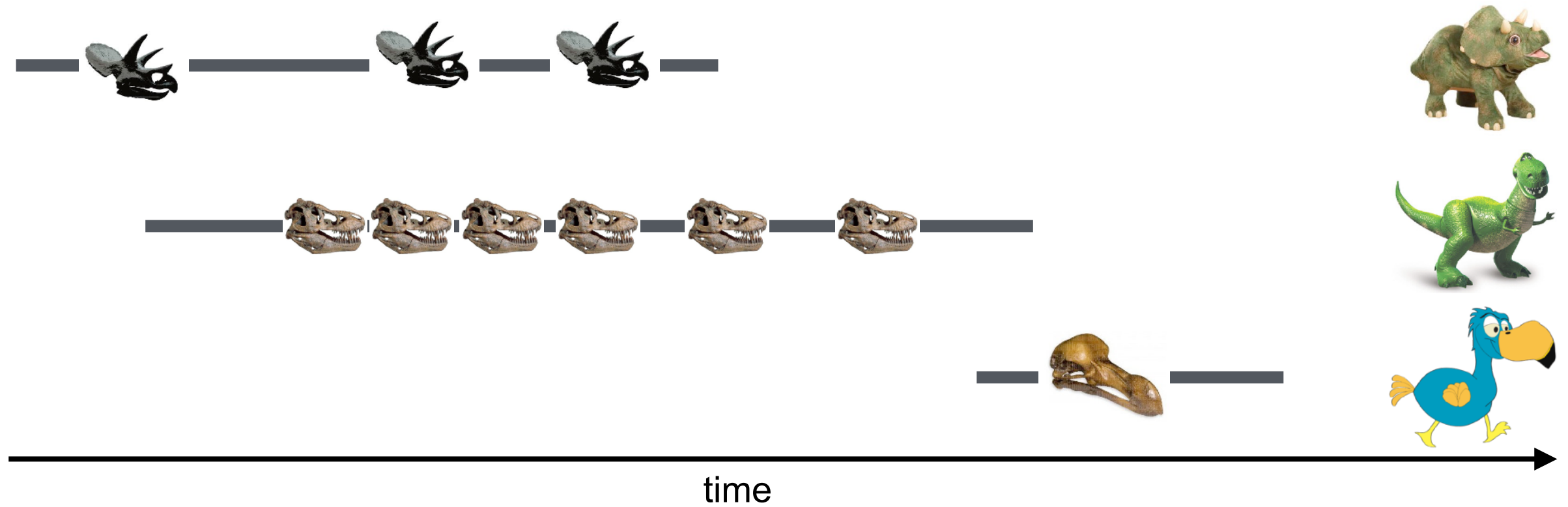


Gamma model of rate heterogeneity

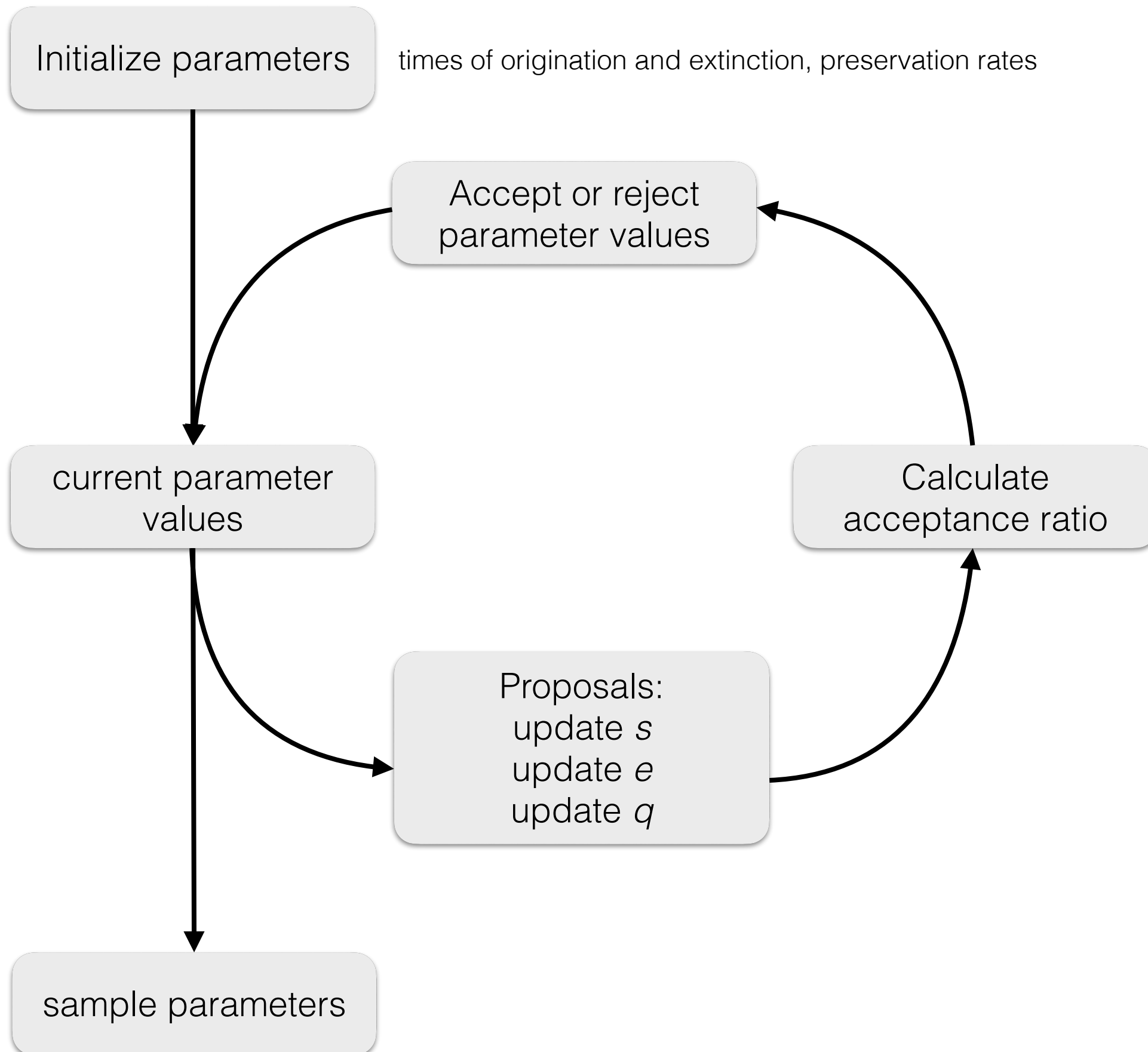
Increasing heterogeneity



Poisson processes of preservation

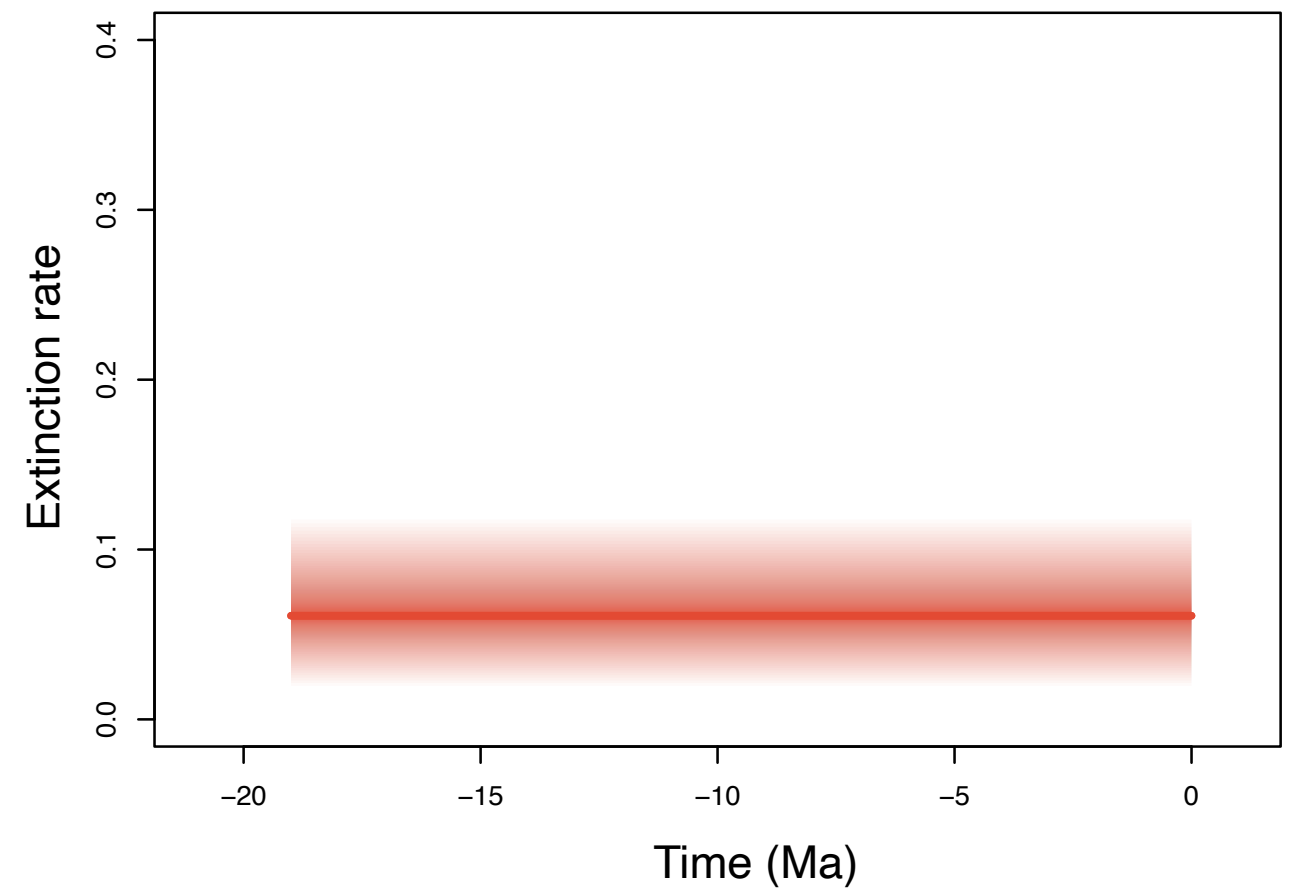
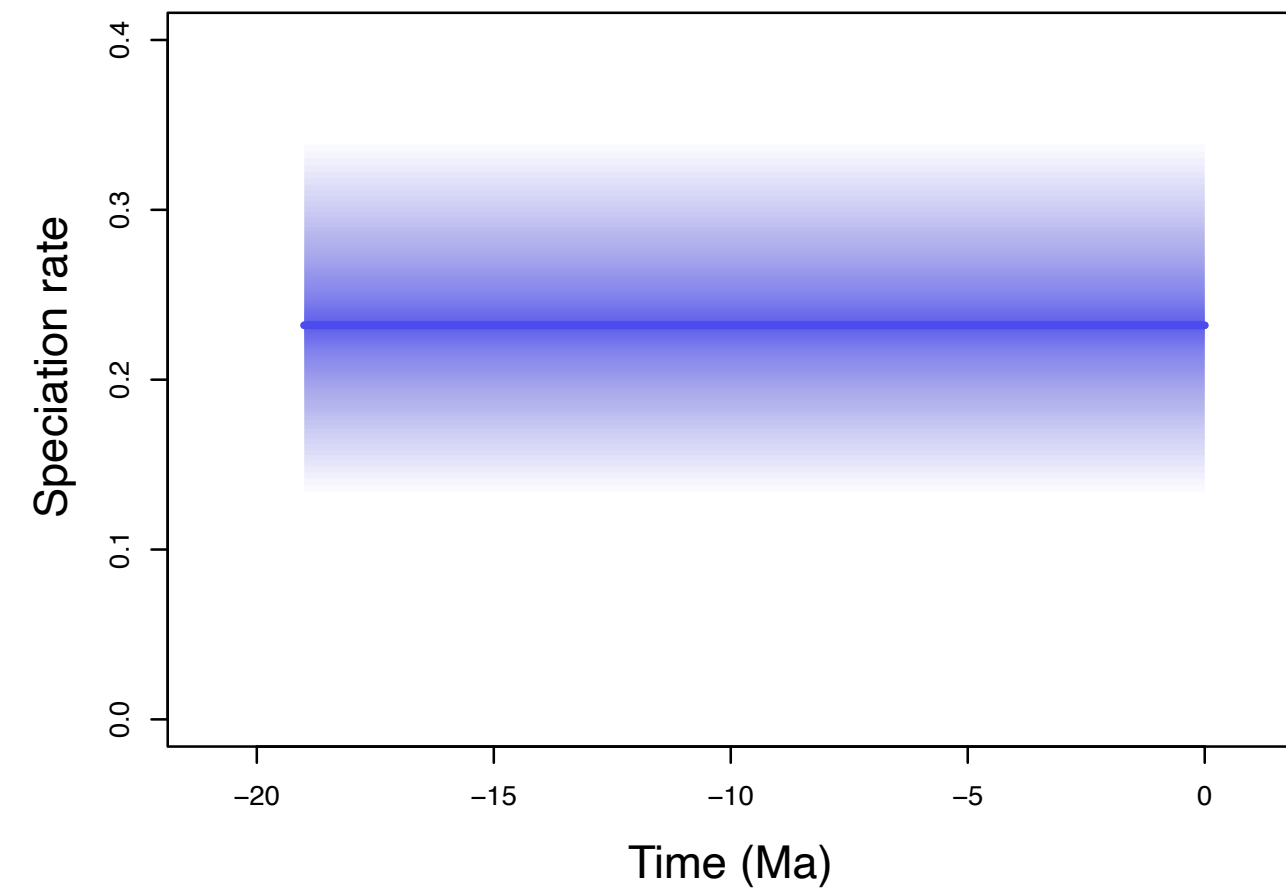


Estimating times of origination, extinction and preservation – MCMC



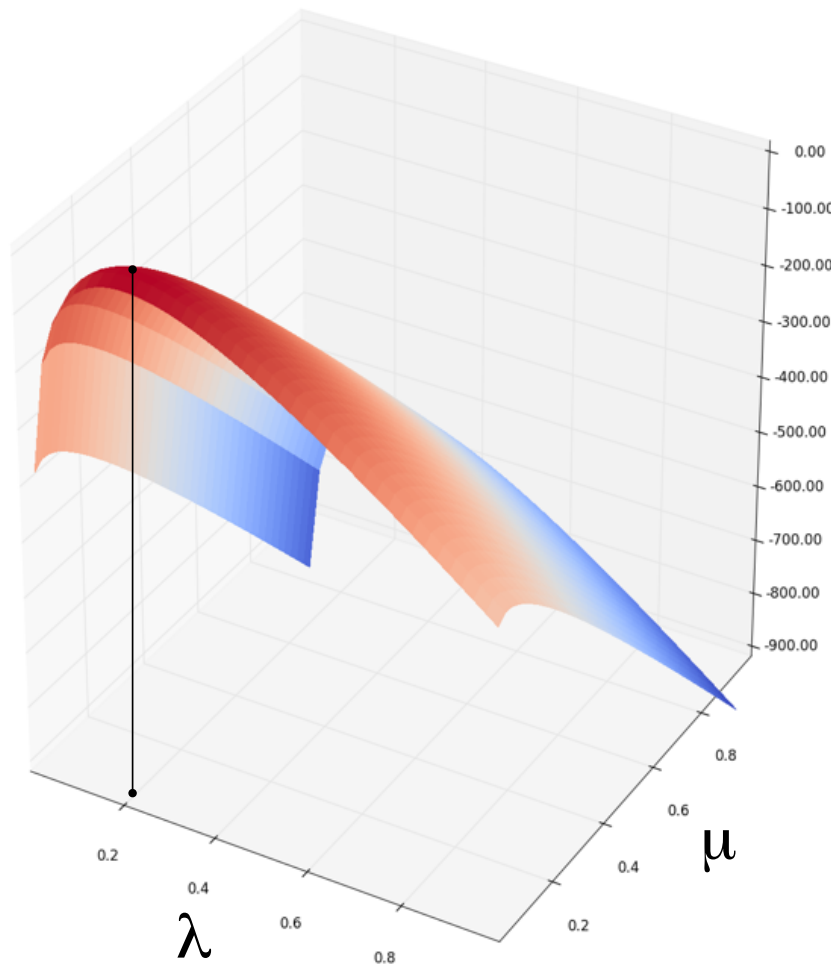
Birth-death models: exploratory (“hypothesis-free”) algorithms

$$\underbrace{P(q, \mathbf{s}, \mathbf{e}, \lambda, \mu | X)}_{\text{posterior}} \propto \underbrace{P(X | q, \mathbf{s}, \mathbf{e})}_{\text{likelihood}} \times \underbrace{P(\mathbf{s}, \mathbf{e} | \lambda, \mu)}_{\text{birth-death prior}} \times \underbrace{P(q)P(\lambda, \mu)}_{\text{other (hyper)priors}}$$

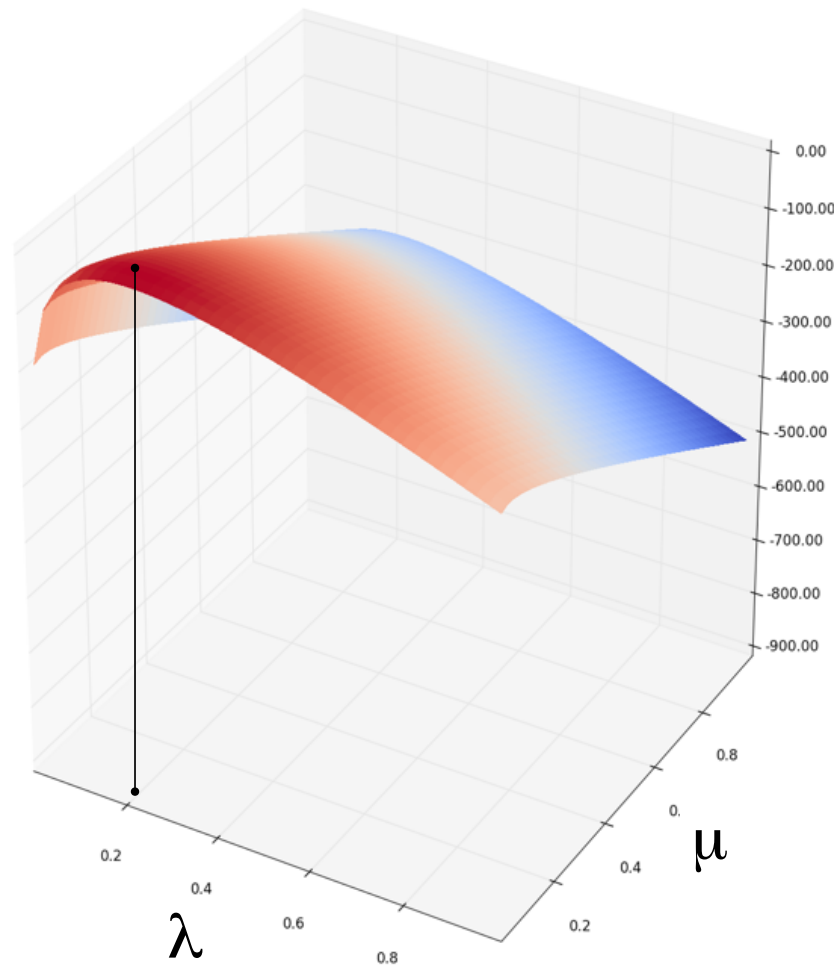


Robustness to incomplete taxon sampling

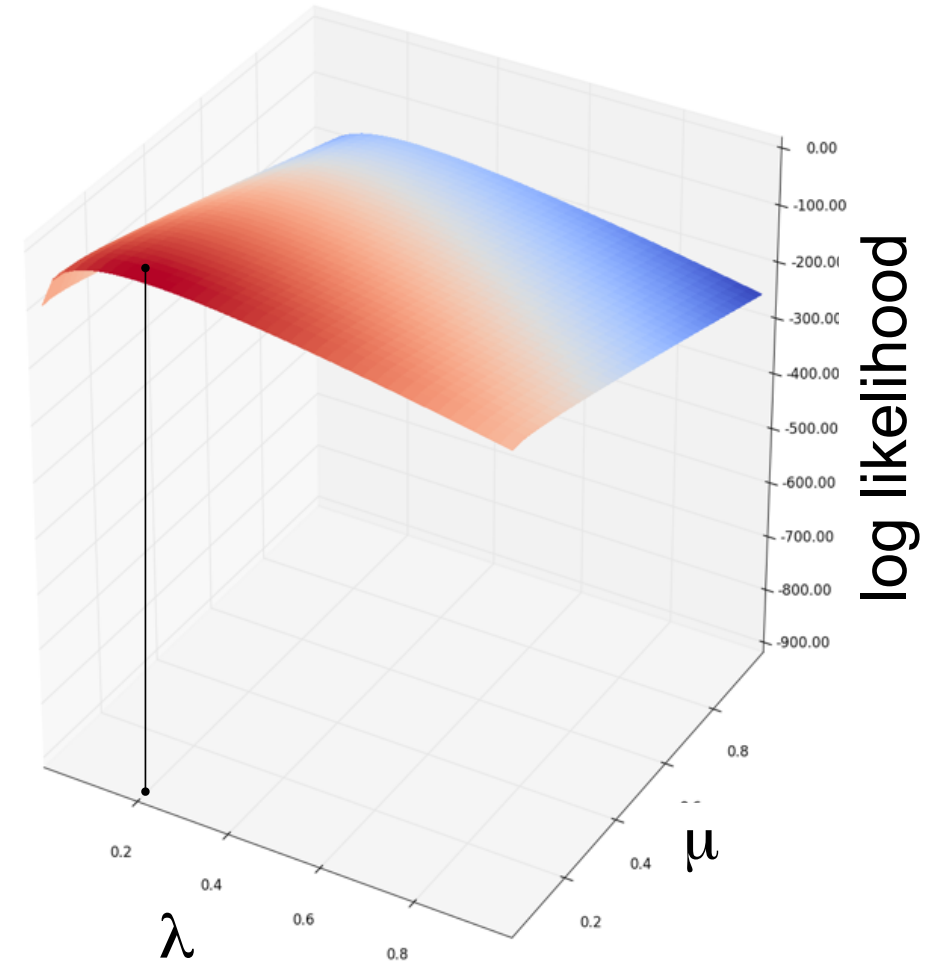
sampling: 100%



sampling: 50%



sampling: 25%

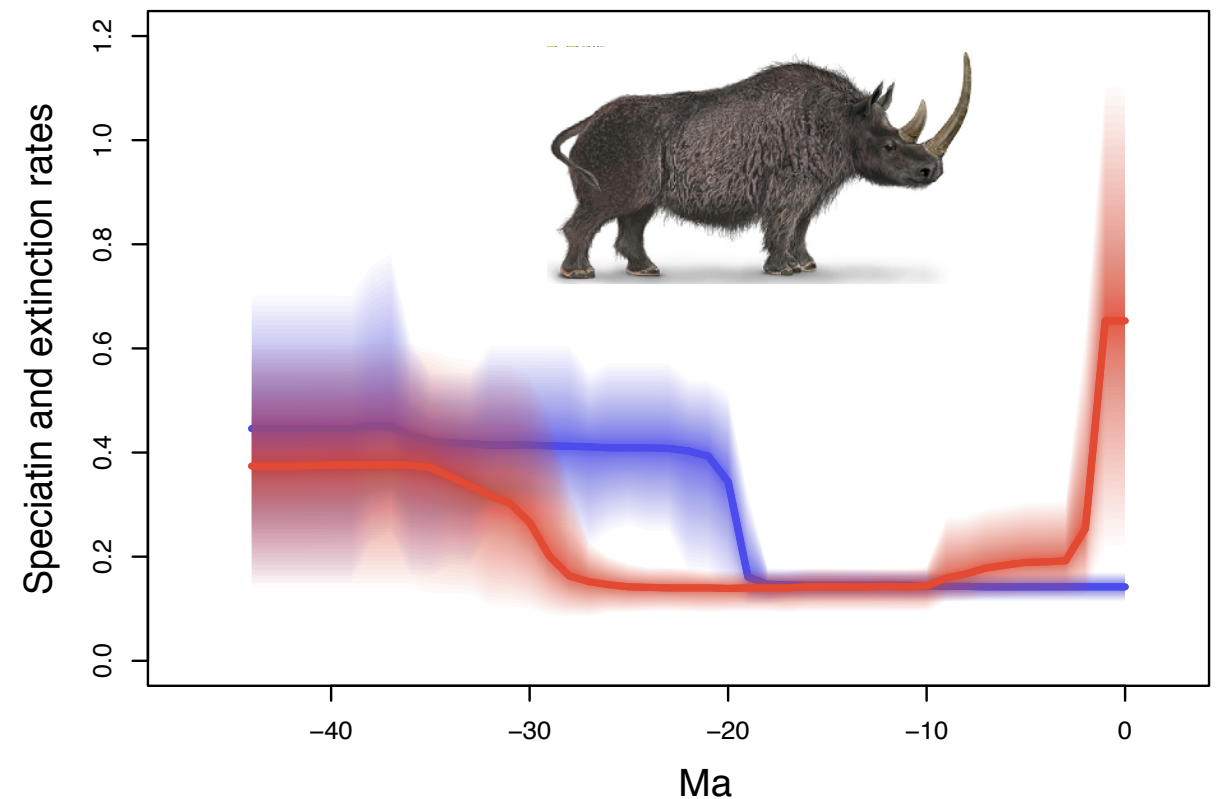
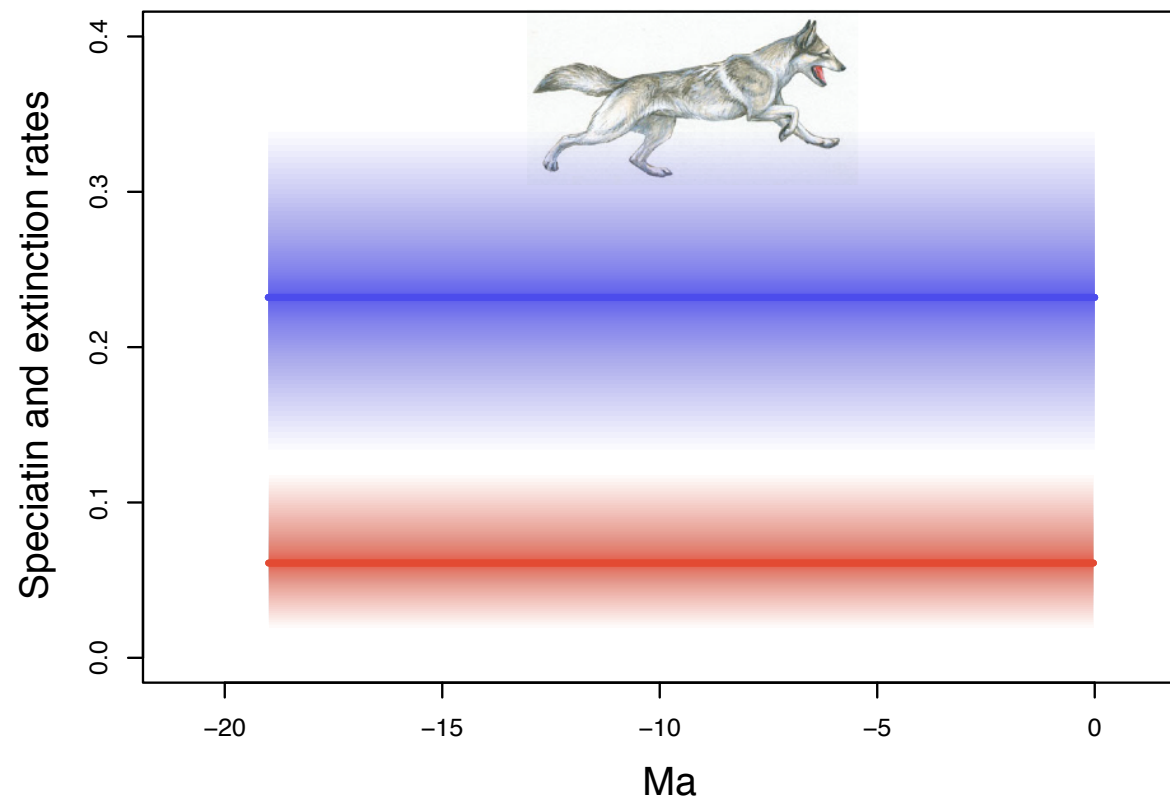


Random taxon sampling does not bias the estimation of speciation and extinction rates

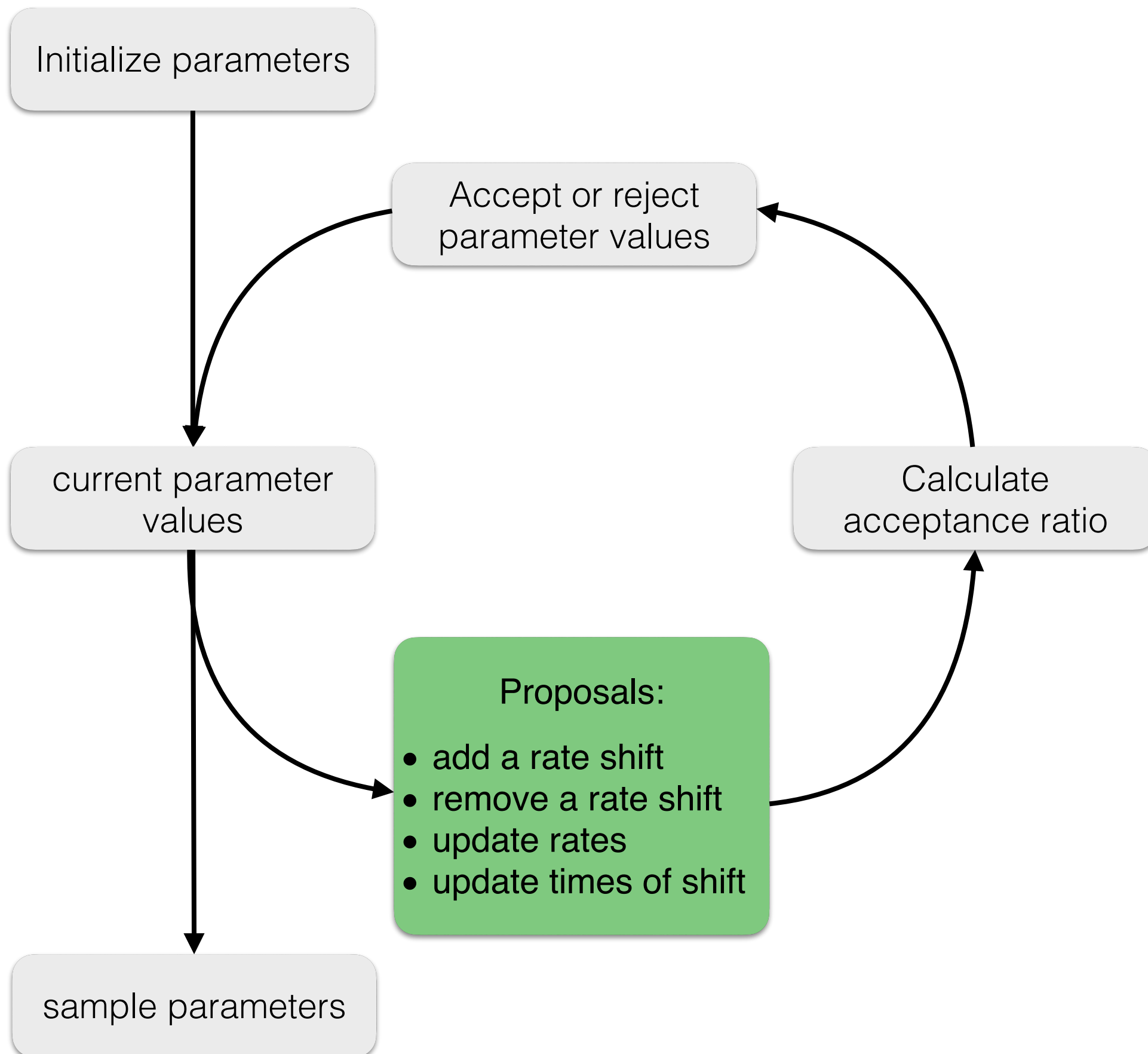
Birth-death models: exploratory (“hypothesis-free”) algorithms

$$\underbrace{P(q, \mathbf{s}, \mathbf{e}, \lambda, \mu | X)}_{\text{posterior}} \propto \underbrace{P(X | q, \mathbf{s}, \mathbf{e})}_{\text{likelihood}} \times \underbrace{P(\mathbf{s}, \mathbf{e} | \lambda, \mu)}_{\text{birth-death prior}} \times \underbrace{P(q)P(\lambda, \mu)}_{\text{other (hyper)priors}}$$

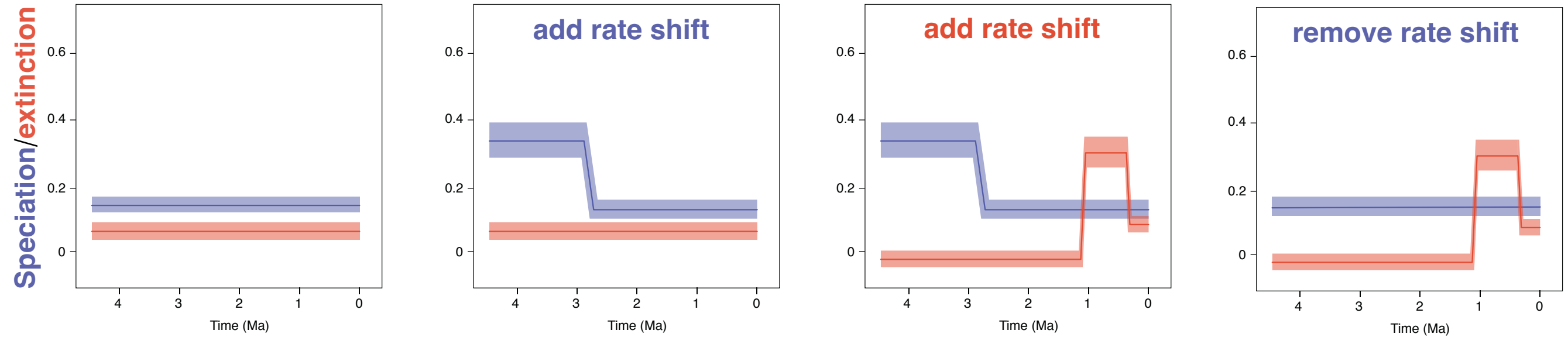
Reversible-jump
MCMC



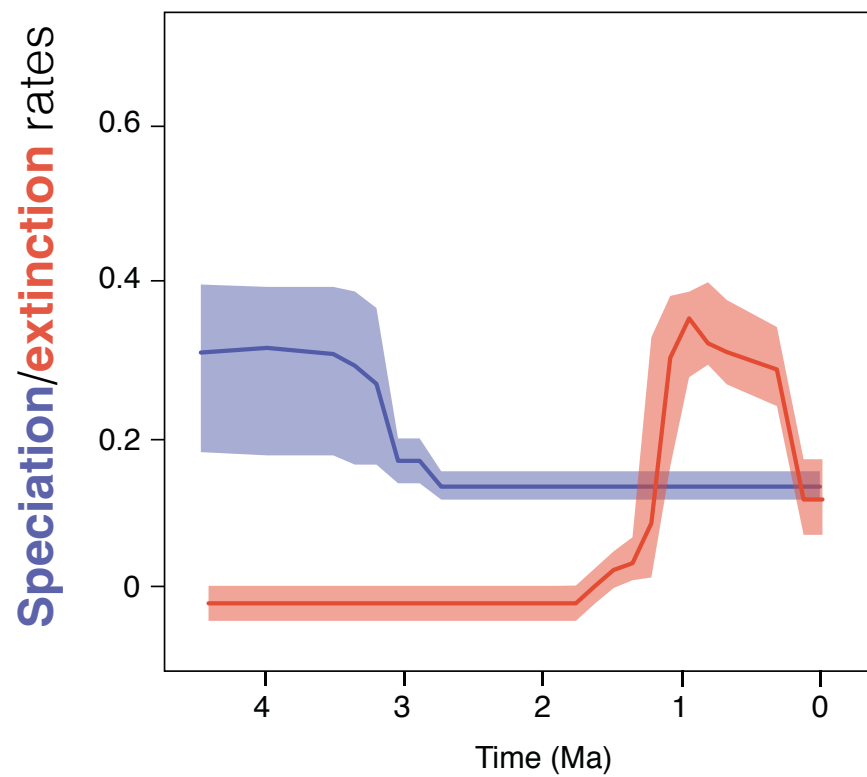
Estimating rate heterogeneity through time – RJMCMC



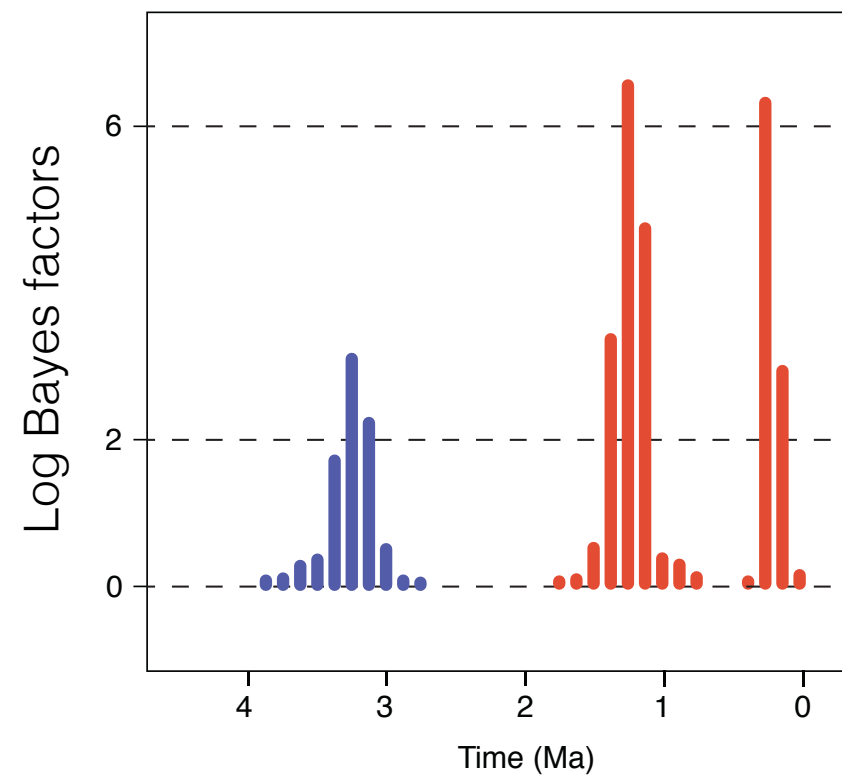
Estimating rate heterogeneity through time – RJMCMC



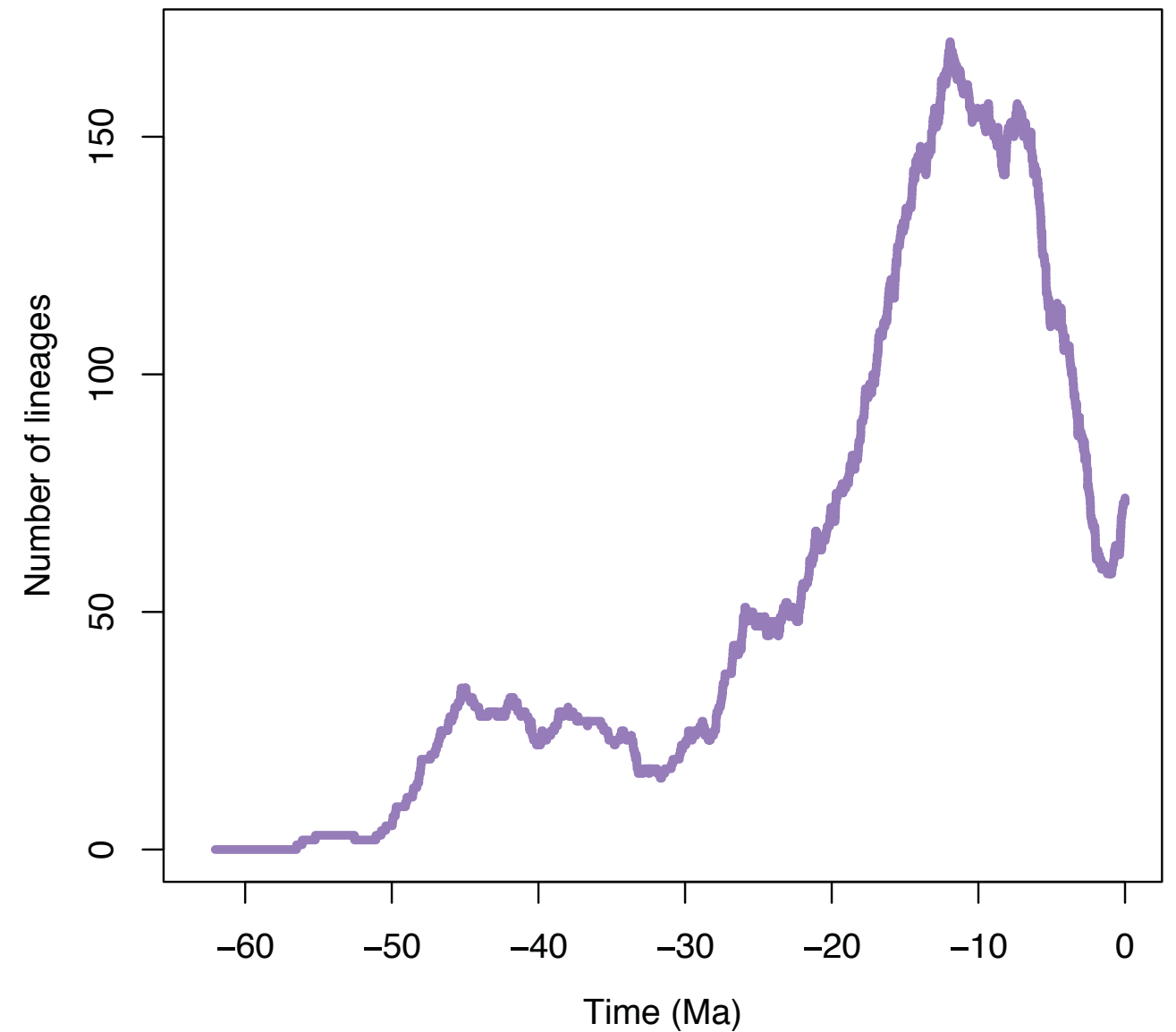
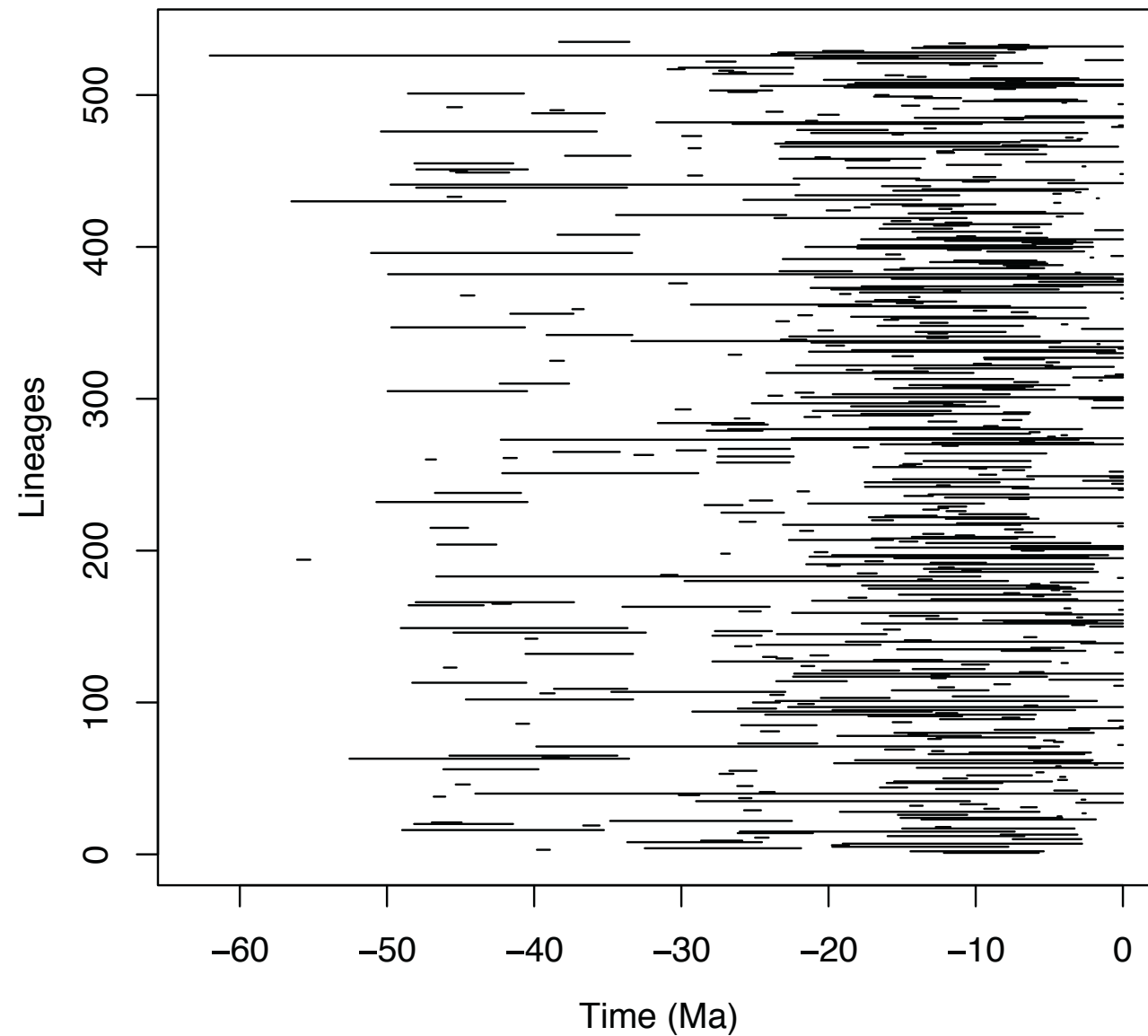
Marginal rates



Times of rate shifts



Diversification and extinction of marine mammals



C Pimiento

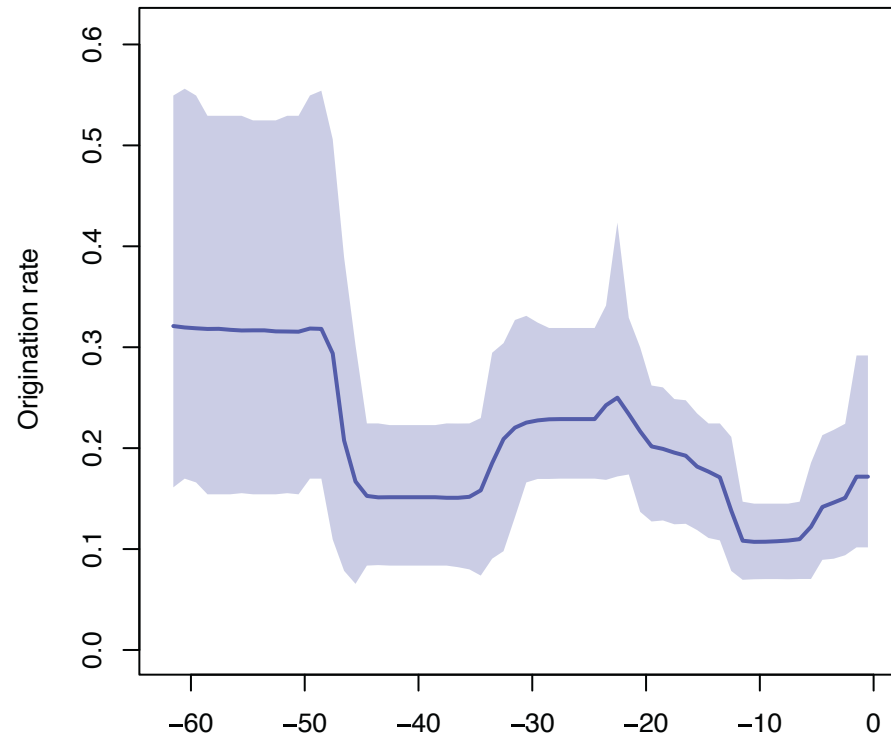


Pimiento et al. 2017 Nat Ecol Evol

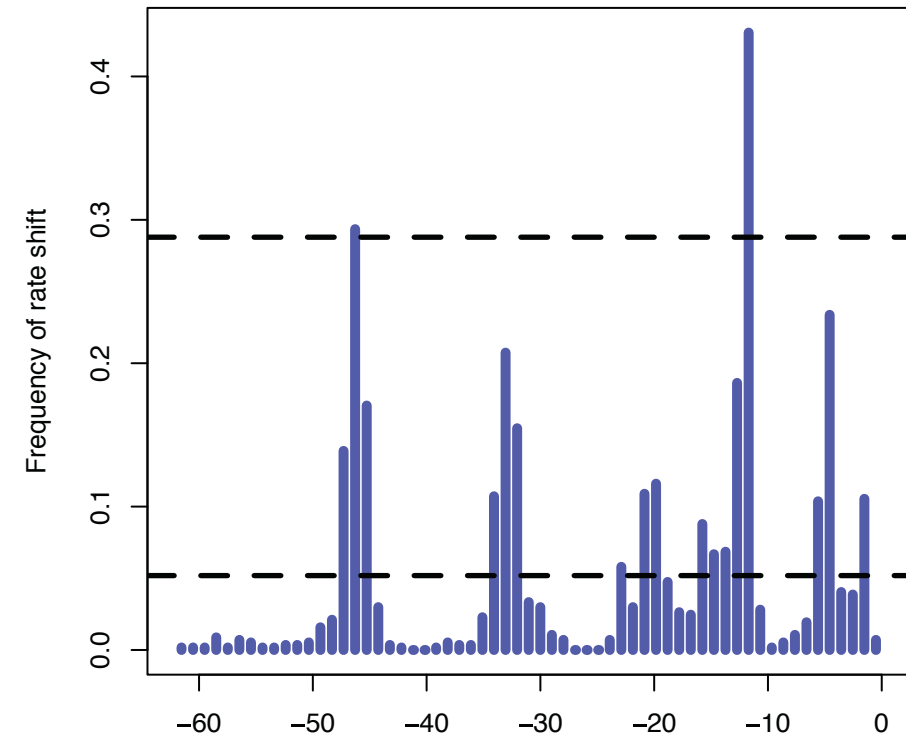
Diversification and extinction of marine mammals

Origination

Marginal origination and extinction rates



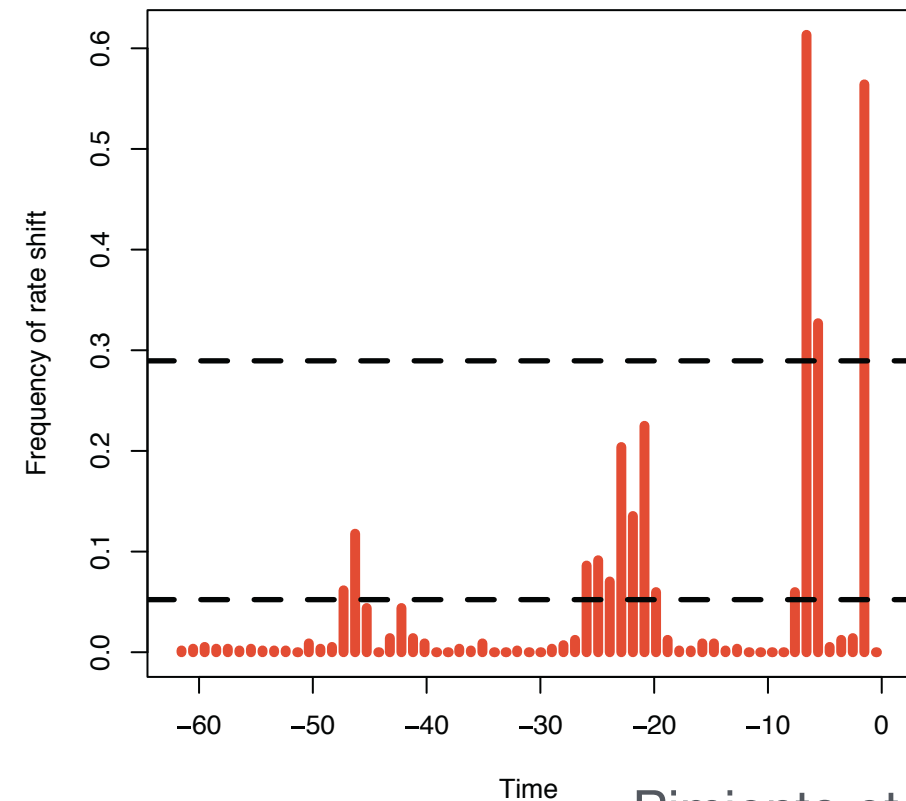
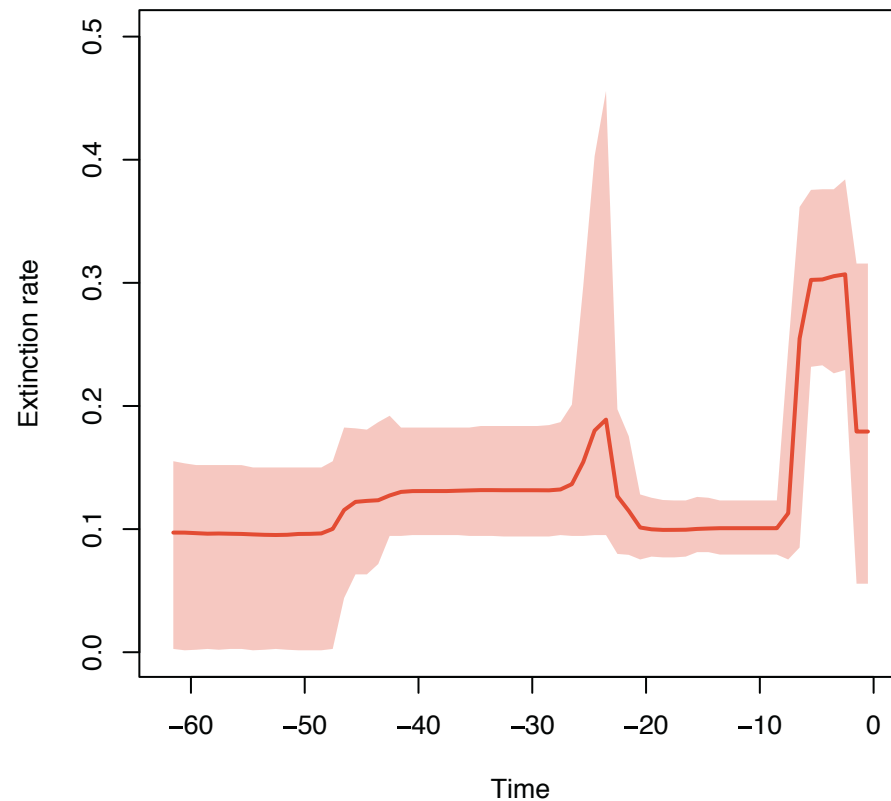
Estimated times of rate shift



Strong support for a rate shift

Significant rate shift

Extinction



Pimiento et al. 2017 Nat Ecol Evol

Hyper-prior distributions on the rate parameters

$$P(s, e, q, \lambda, \mu | x) \propto P(x | s, e, q) \times P(s, e | \lambda, \mu) \times P(q) P(\lambda, \mu)$$

POSTERIOR

LIKELIHOOD

PRIOR

HYPERPRIORS



Gamma prior on preservation rate



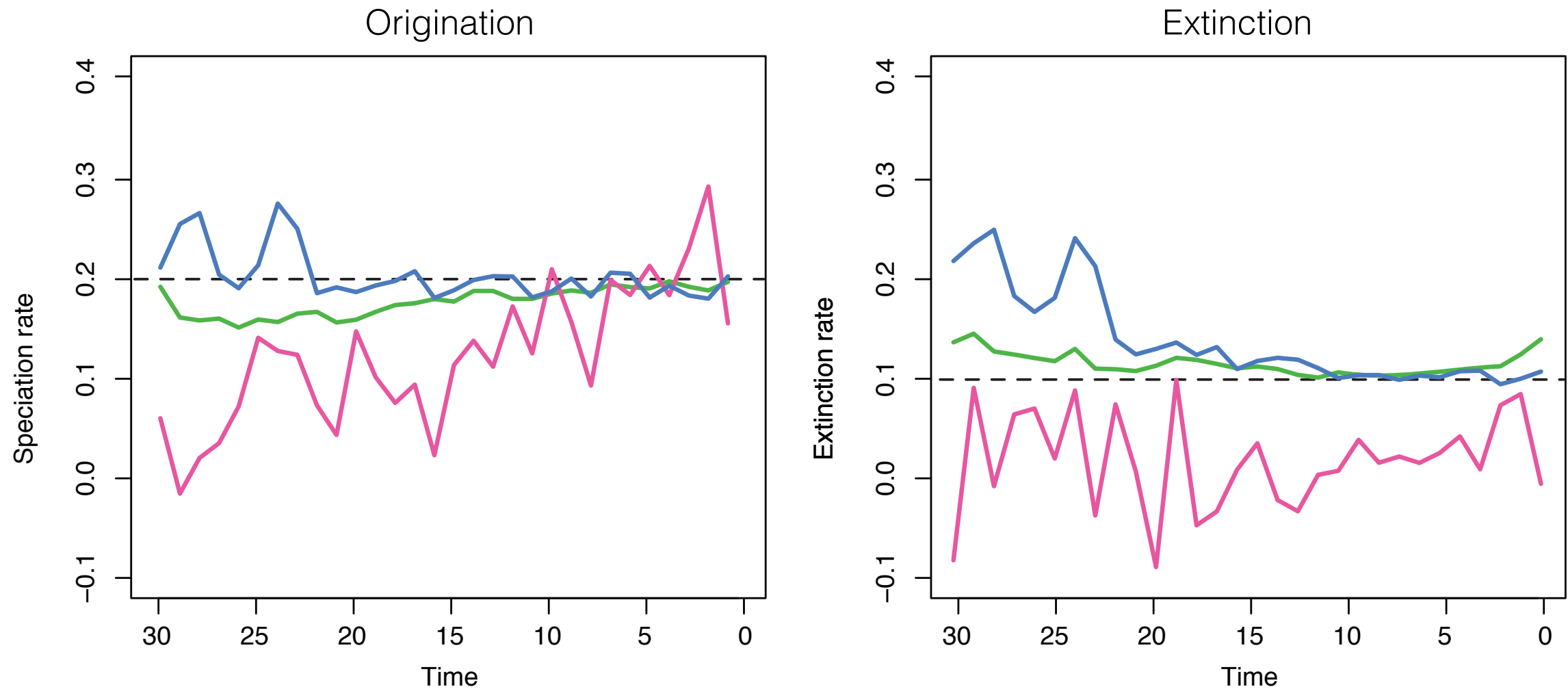
Uniform prior on alpha (rate heterogeneity)



Gamma or half-Cauchy priors on BD rates

Effects of PyRate's regularization through RJMCMC

Constant birth-death simulation with constant, low preservation



Mean per capita (Foote 2000)

Three-timer (Alroy 2008)

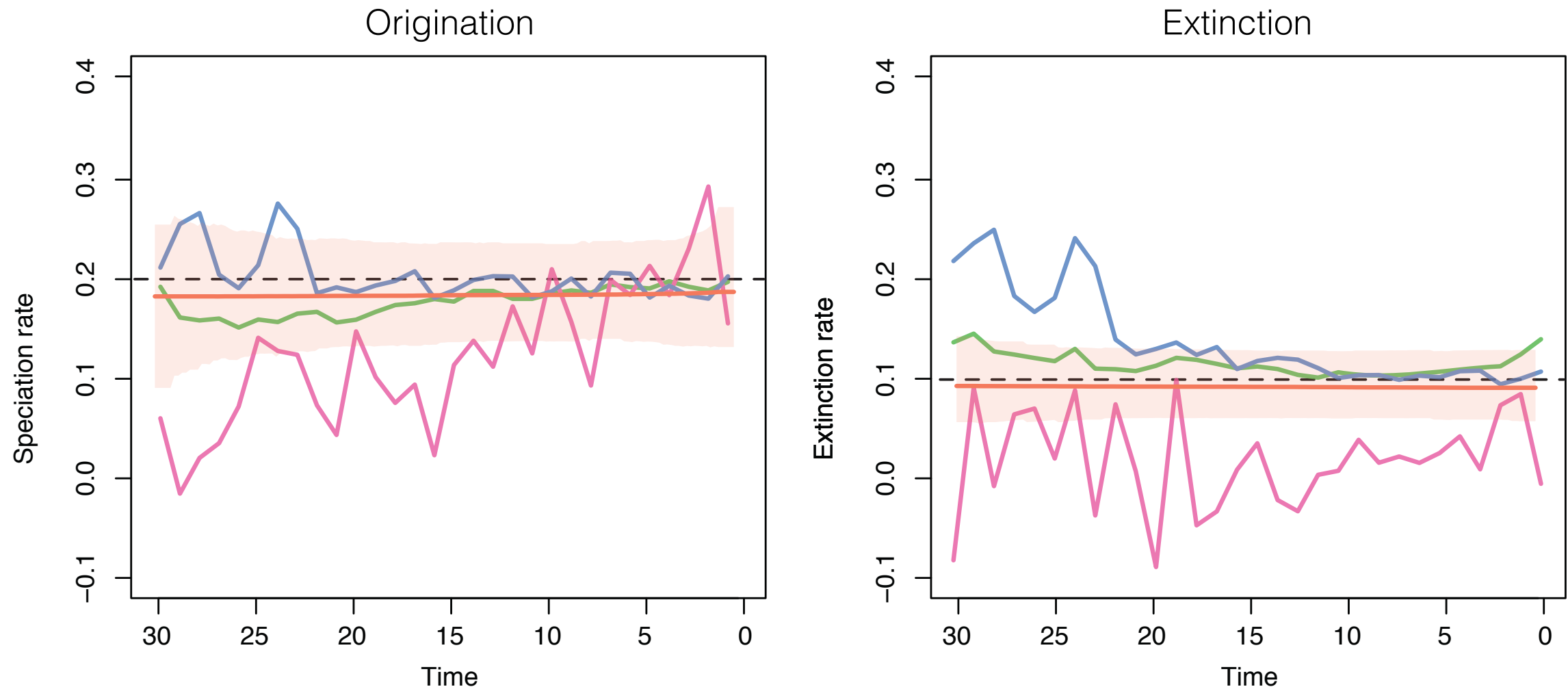
CMR (Liow & Finarelli 2014)



T M Smiley

Effects of PyRate's regularization through RJMCMC

Constant birth-death simulation with constant, low preservation



Mean per capita (Foote 2000)

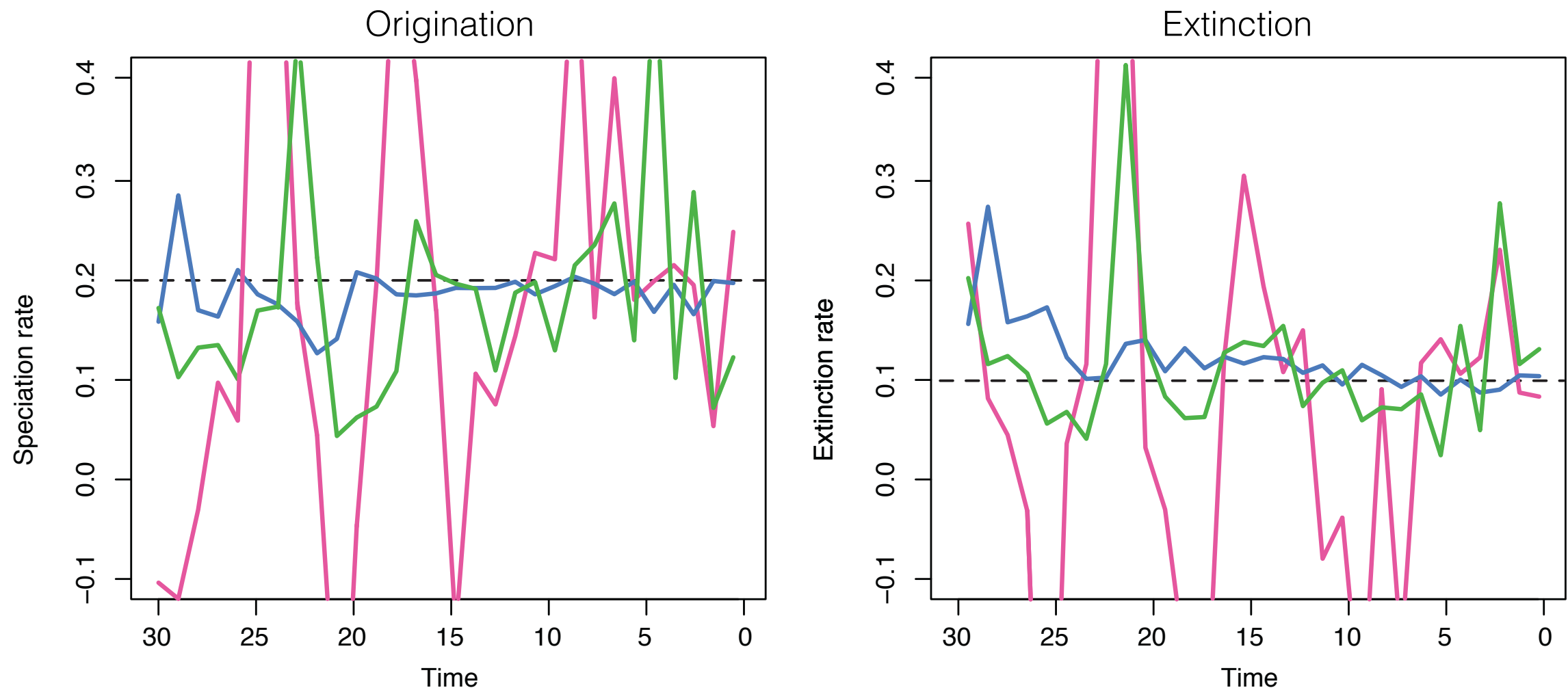
Three-timer (Alroy 2008)

CMR (Liow & Finarelli 2014)

PyRate

Effects of PyRate's regularization through RJMCMC

Constant birth-death simulation with time-variable preservation



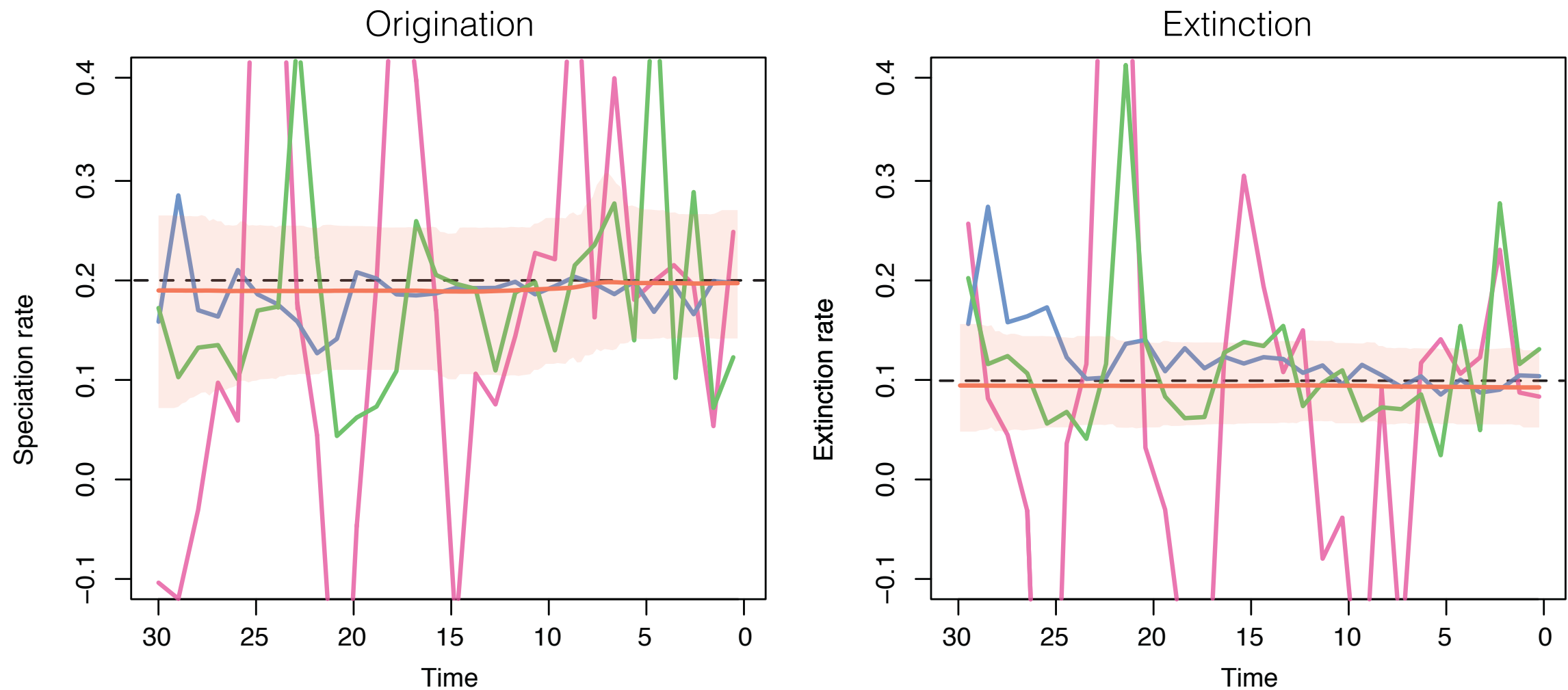
Mean per capita (Foote 2000)

Three-timer (Alroy 2008)

CMR (Liow & Finarelli 2014)

Effects of PyRate's regularization through RJMCMC

Constant birth-death simulation with time-variable preservation



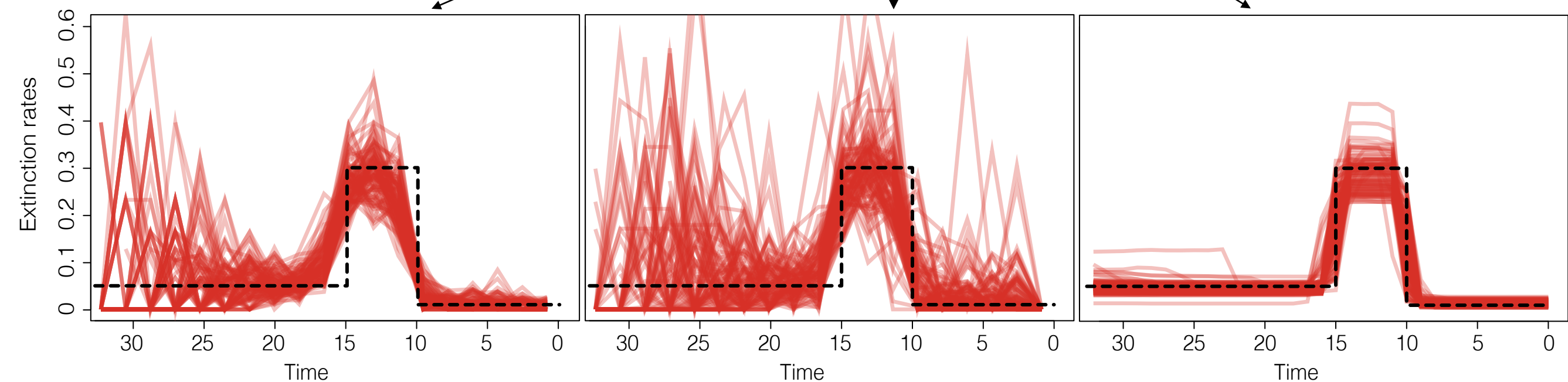
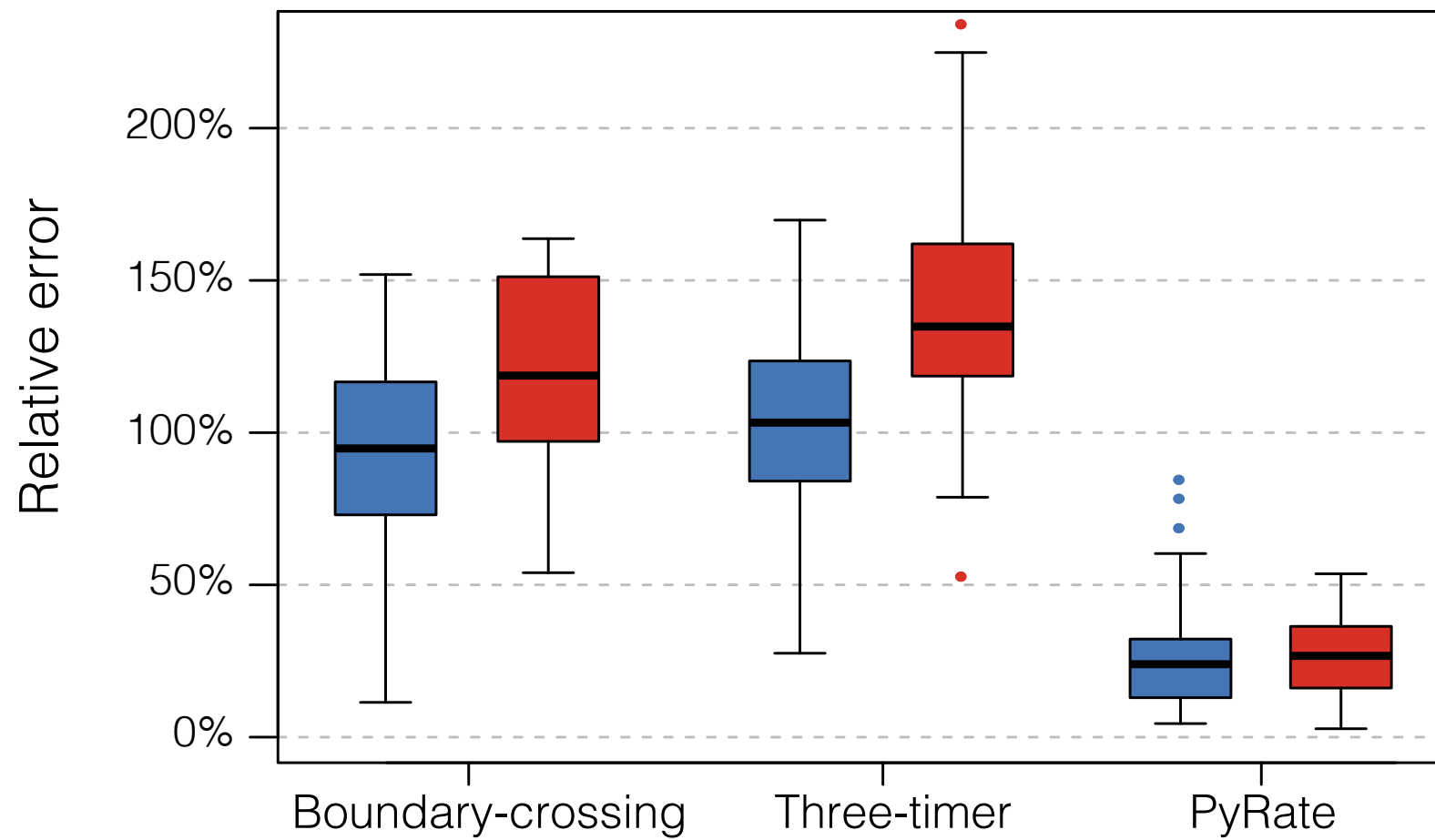
Mean per capita (Foote 2000)

Three-timer (Alroy 2008)

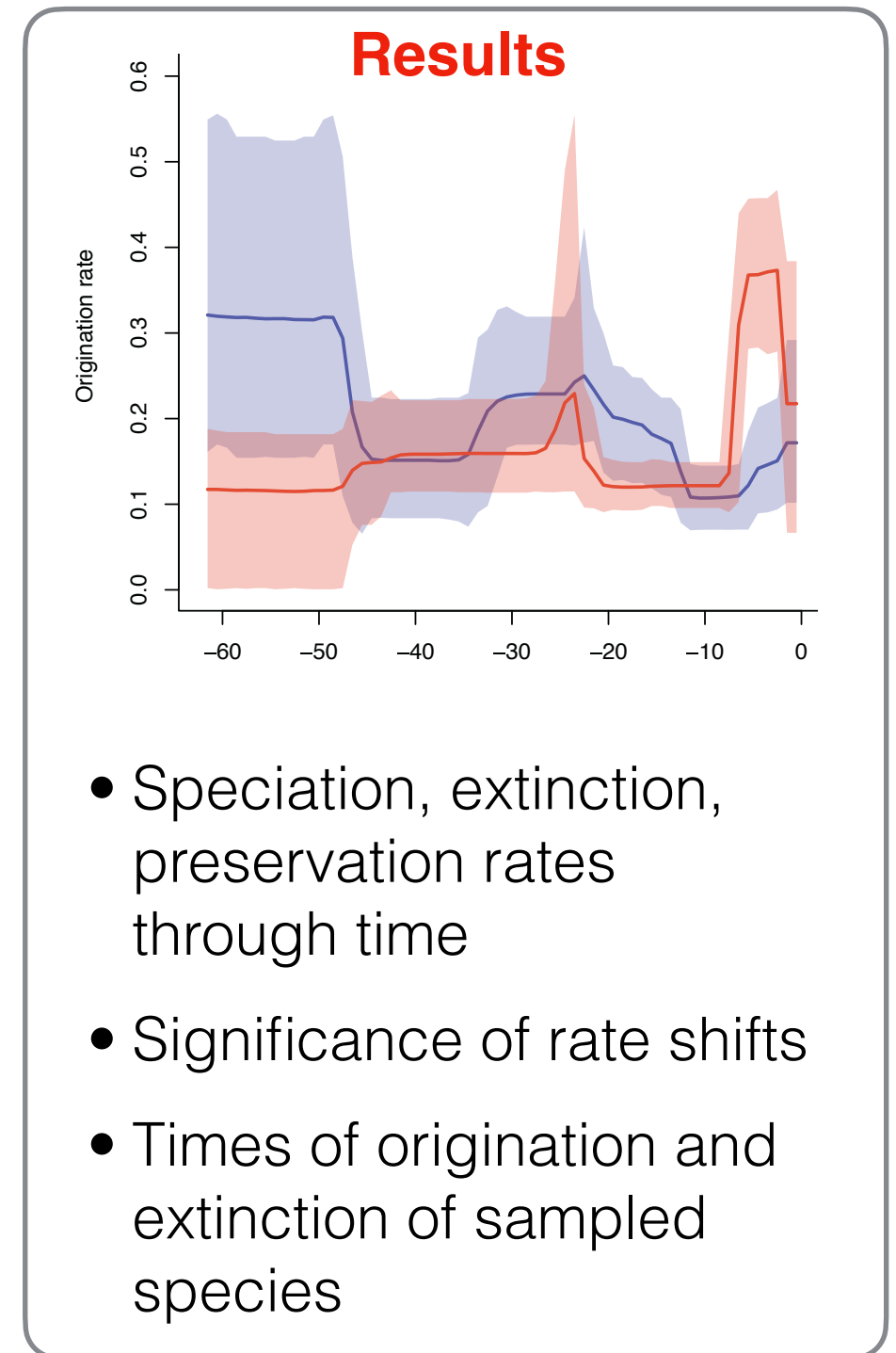
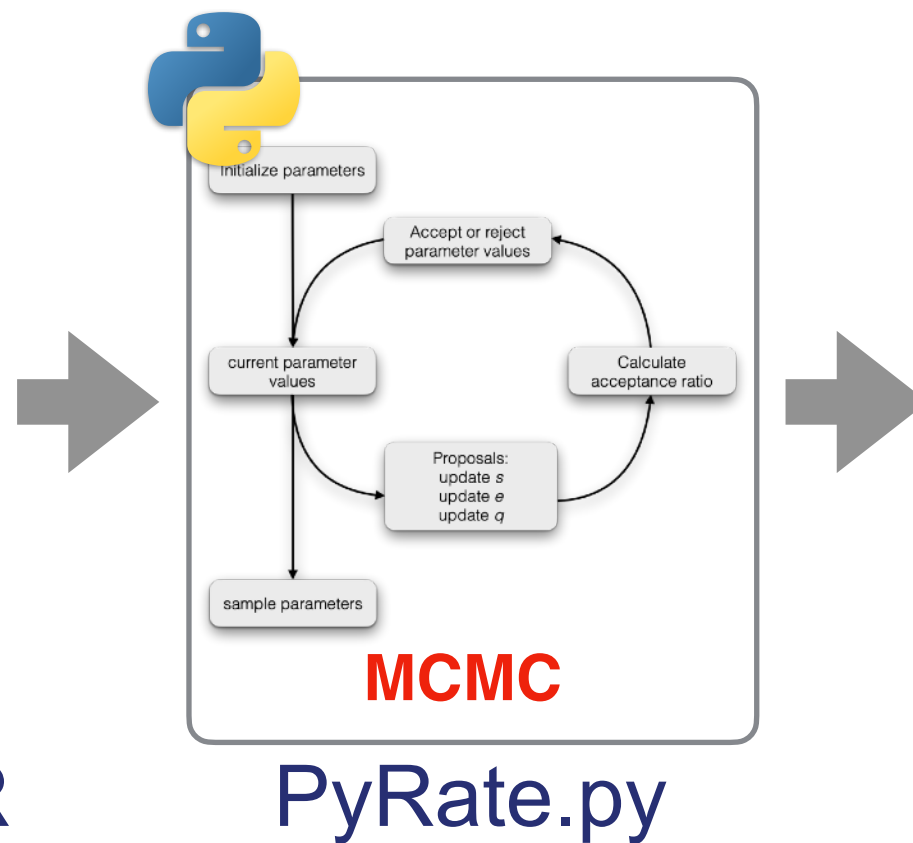
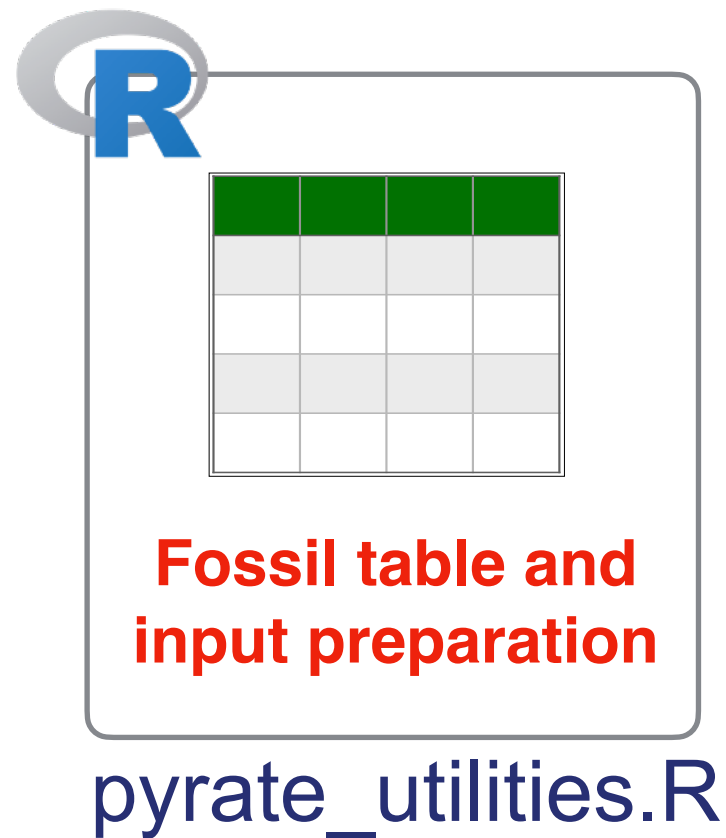
CMR (Liow & Finarelli 2014)

PyRate

Error in estimated **Speciation** & **extinction** rates



How PyRate works



How PyRate works

Taxon	Status	MinAge	MaxAge
<i>Ailurus</i>	Extant	0.6	1.3
<i>Alopecocyon</i>	Extinct	9.5	10.35
<i>Alopecocyon</i>	Extinct	9.7	11.11
...	...	...	...

Fossil occurrence data with age range and info on whether it's extant or extinct



**Parse fossil
table and create
PyRate input file**

```
1 # load PyRate utilities
2
3 source("../PyRate-master/pyrate_utilities.r")
4 extract.ages(file = "path_to_your_fossil_table/Ursidae.txt",
5              replicates = 10, # specify number of age randomizations
6              cutoff = 10 # drop occurrences with wide age range (e.g. 10 myr)
7              )
8
9
```

How PyRate works



**Run PyRate in a
Terminal window**

A screenshot of a macOS terminal window titled 'PyRate — -zsh — 110x40'. The terminal shows two commands being executed: first, 'cd Software/PyRate' which changes the directory, and second, 'python PyRate.py path_to_input/Rhinocerotidae_PyRate.py' which runs the PyRate script with a specific input file path. The prompt changes from '[mbp:~ \$]' to '[mbp:PyRate \$]' after the first command.

```
[mbp:~ $ cd Software/PyRate  
[mbp:PyRate $ python PyRate.py path_to_input/Rhinocerotidae_PyRate.py
```

This will run a default analysis with RJMCMC

How PyRate works



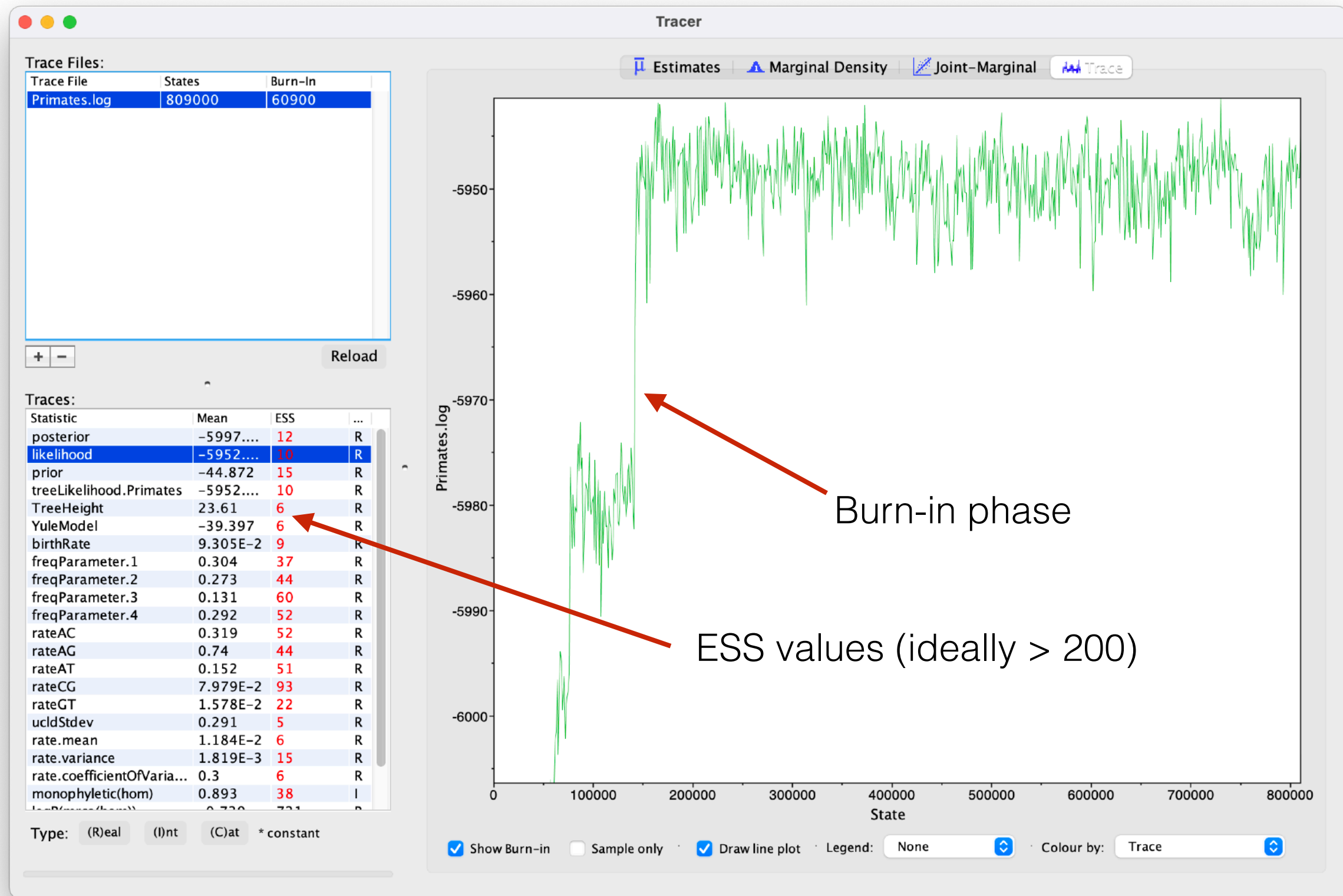
**Add options to the analysis: time
variable preservation rates**

```
PyRate — -zsh — 110x40
[mbp:~ $ cd Software/PyRate
[mbp:PyRate $ python PyRate.py path_to_input/Rhinocerotidae_PyRate.py -qShift path_to_file/epochs.txt
```

Simple text file defining the
time bins for piece-wise
constant preservation rates

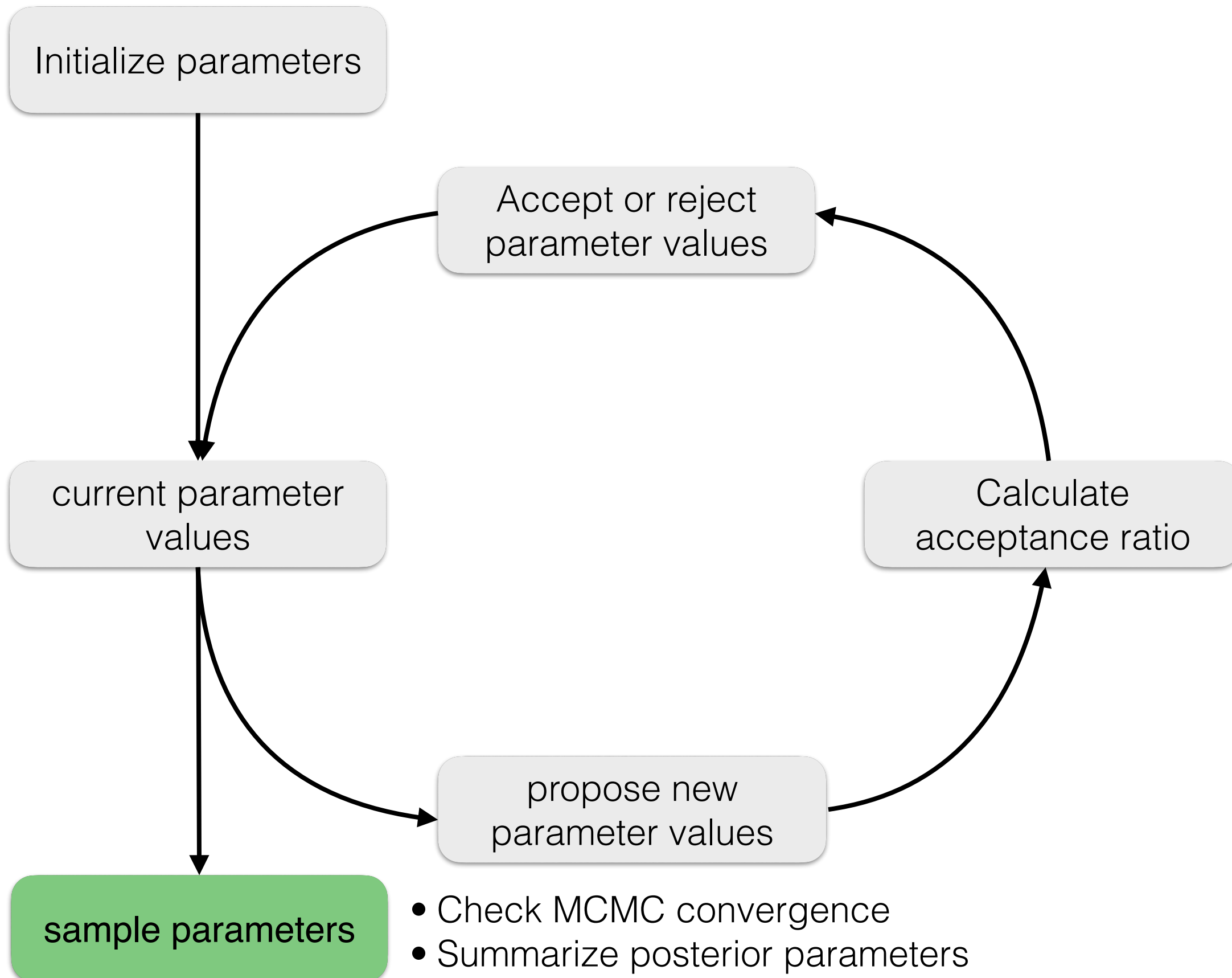
2.58
5.333
23.03
33.9
56.0
66.0

Check MCMC convergence

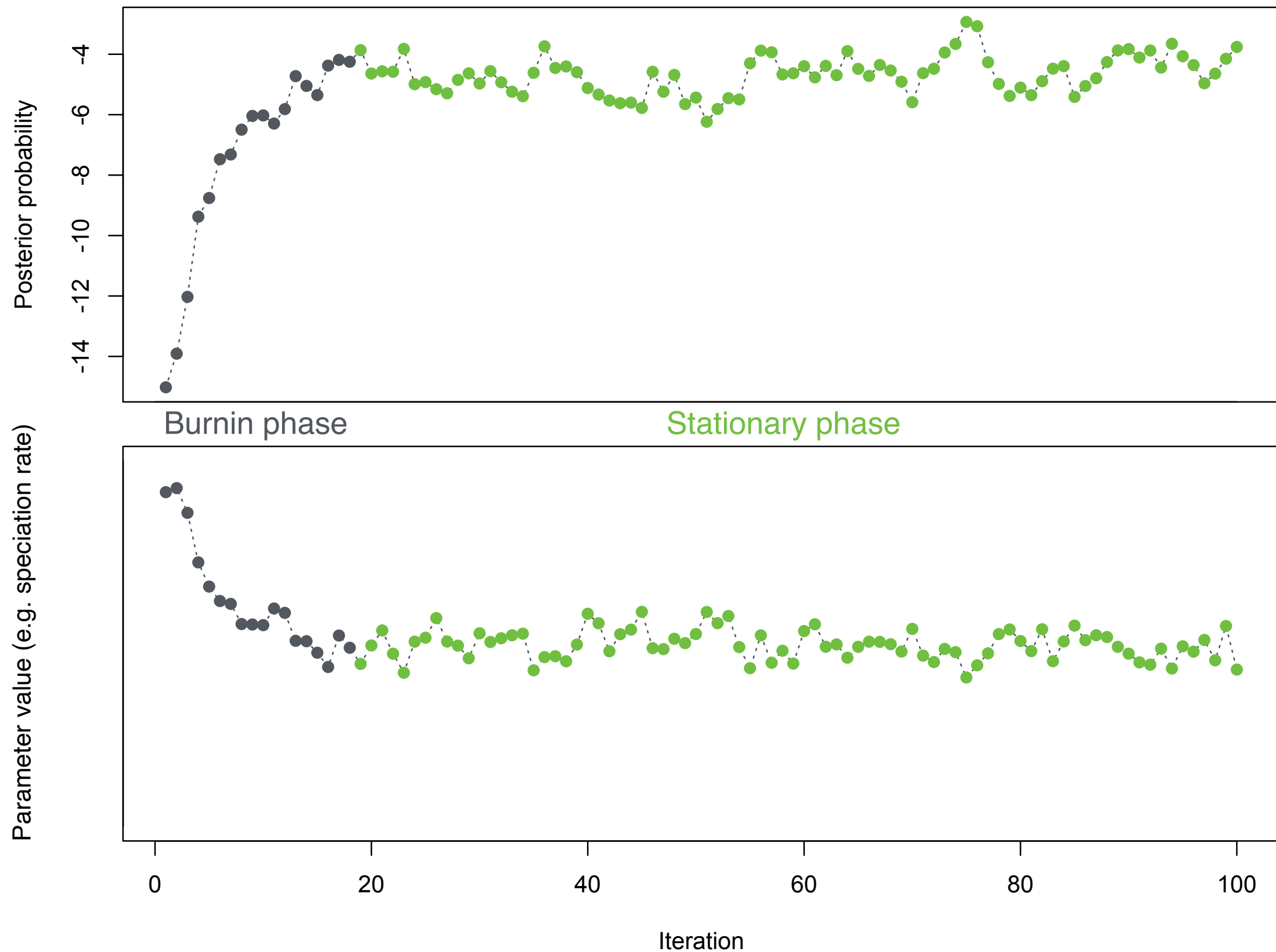


Tracer

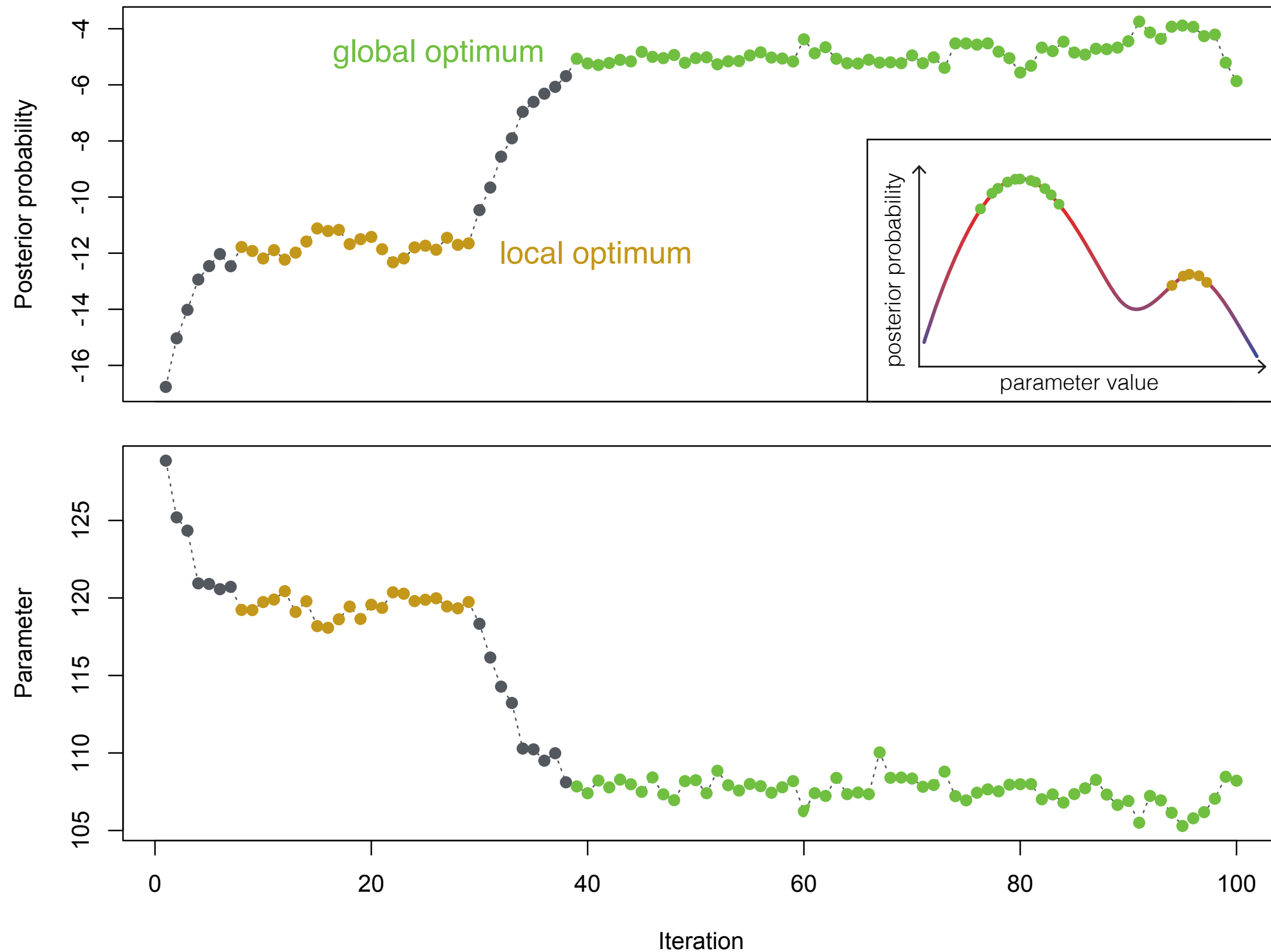
Metropolis-Hastings MCMC



Burn-in and MCMC convergence

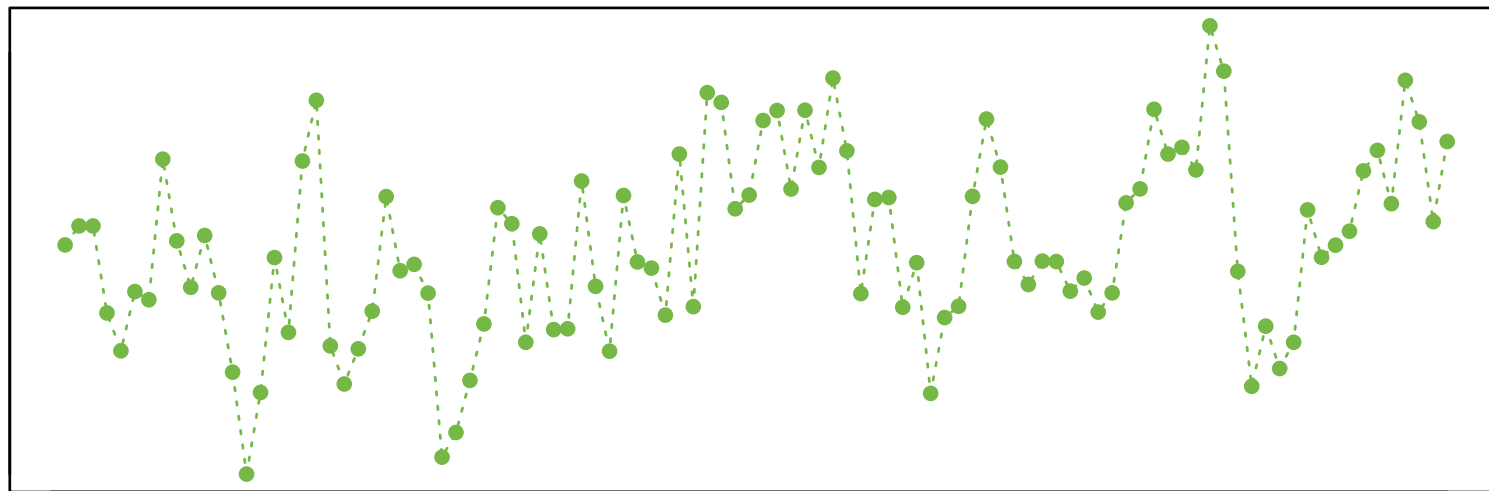


Burn-in and MCMC convergence



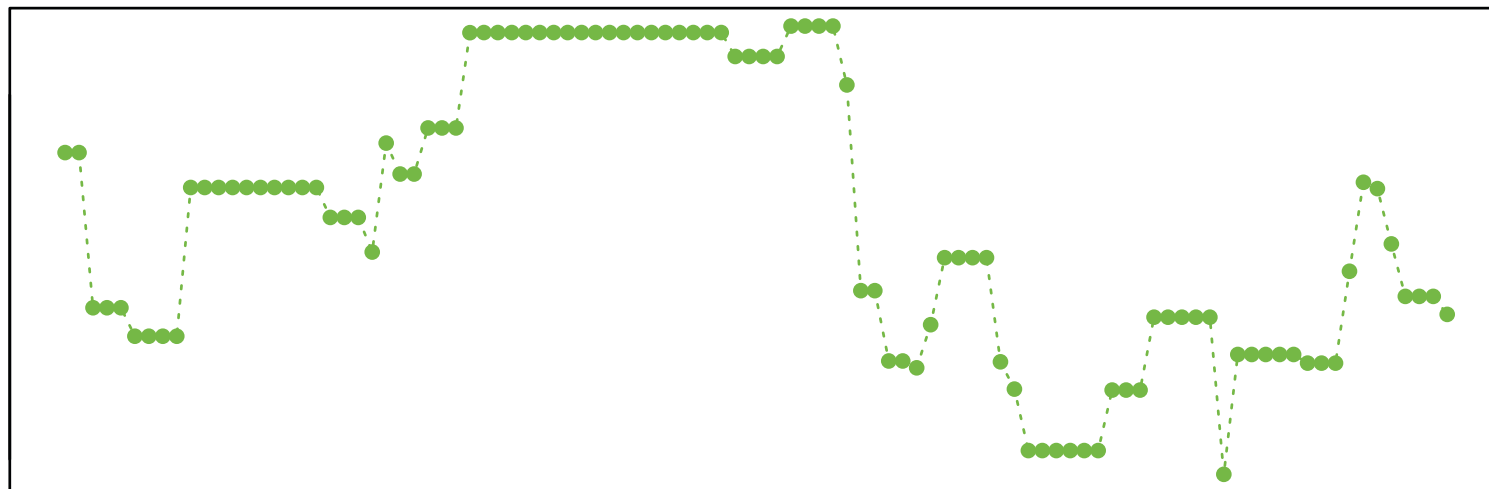
Posterior samples: Effective Sample Size (ESS)

Sampled parameter values



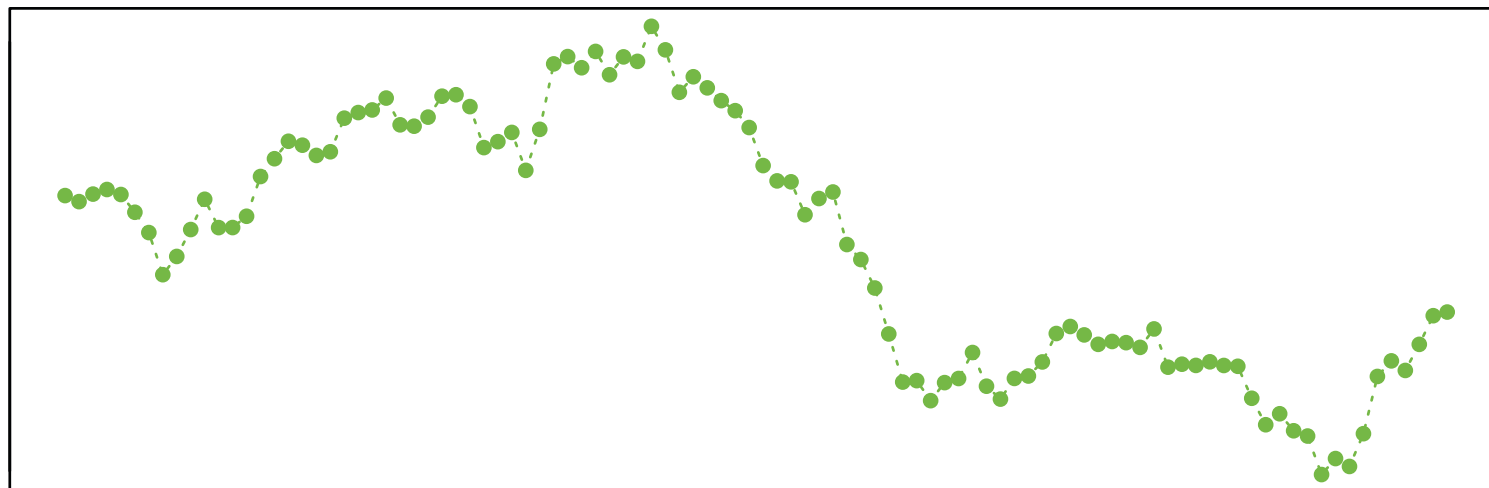
High ESS

Sampled parameter values



Low ESS

Sampled parameter values

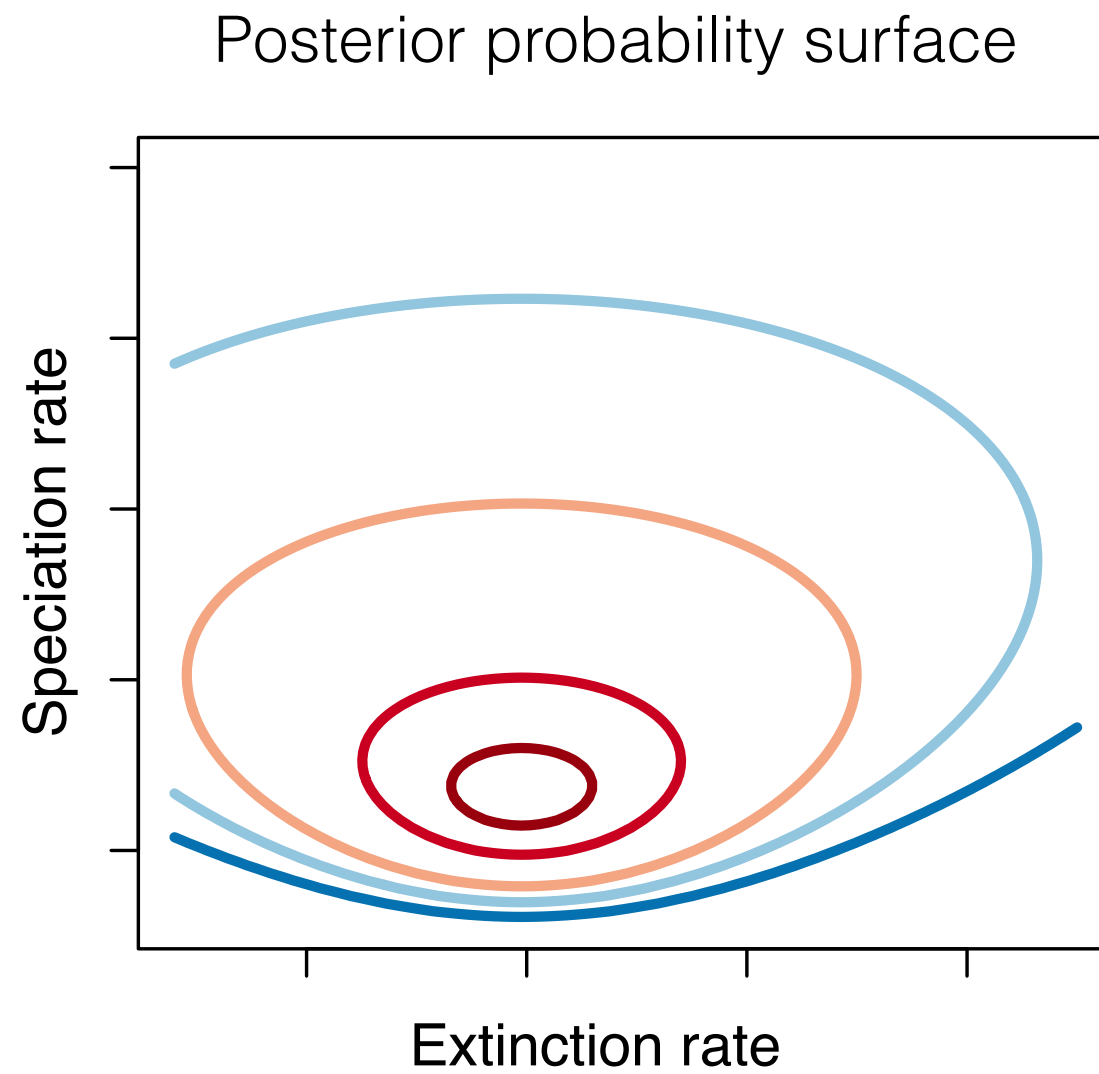


Low ESS

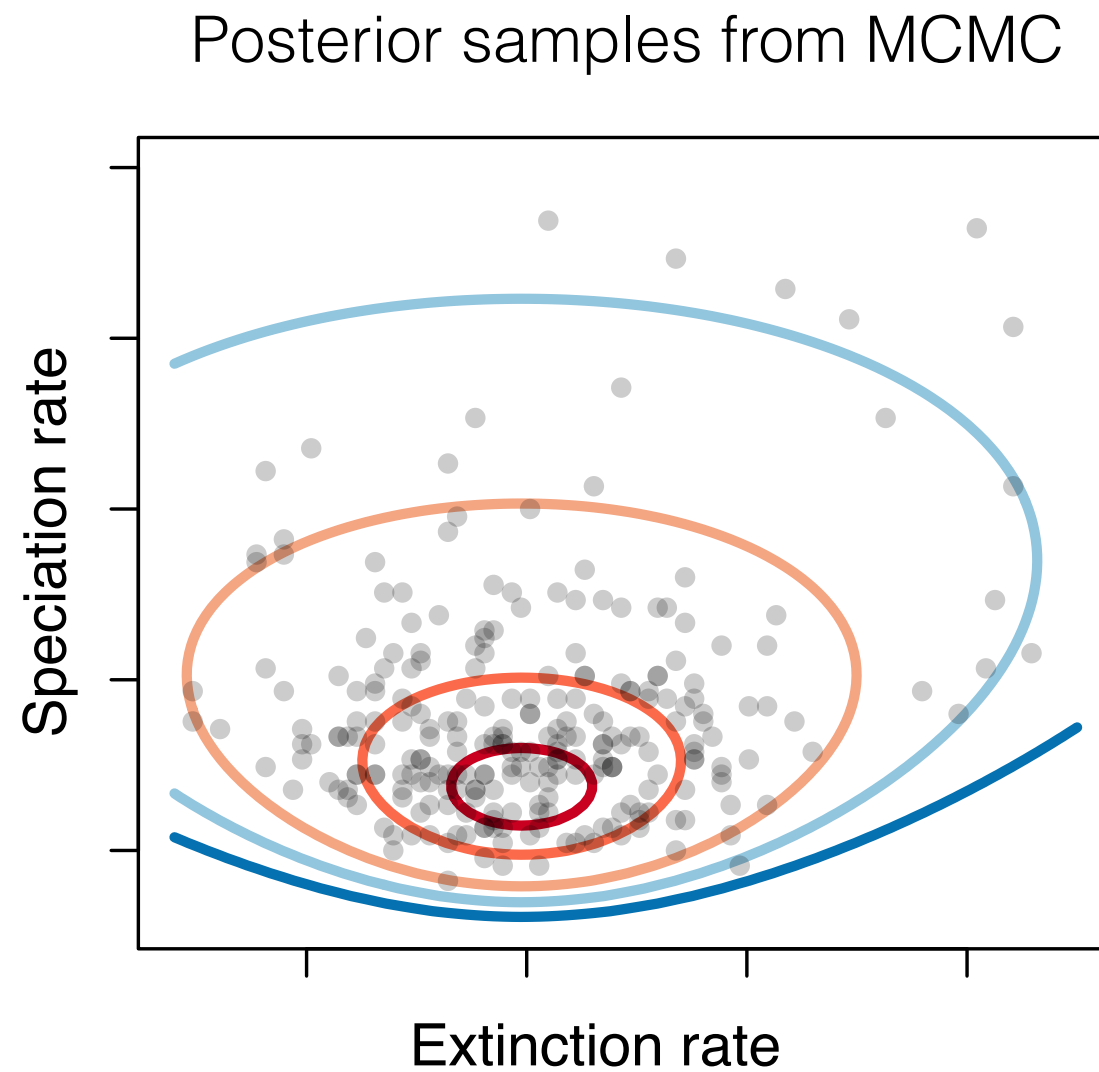
0 20 40 60 80 100

MCMC iteration

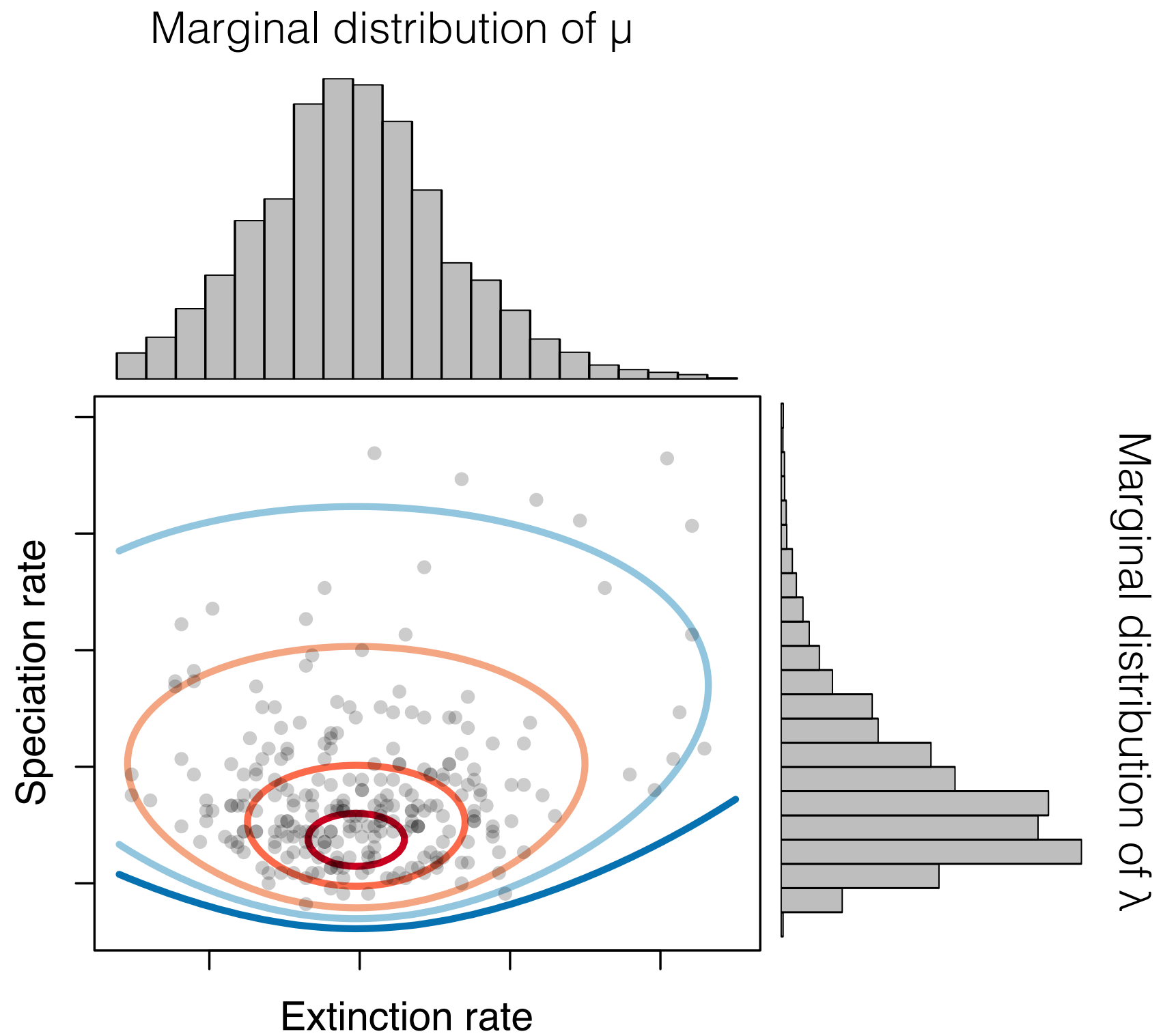
Summarizing MCMC samples



Summarizing MCMC samples



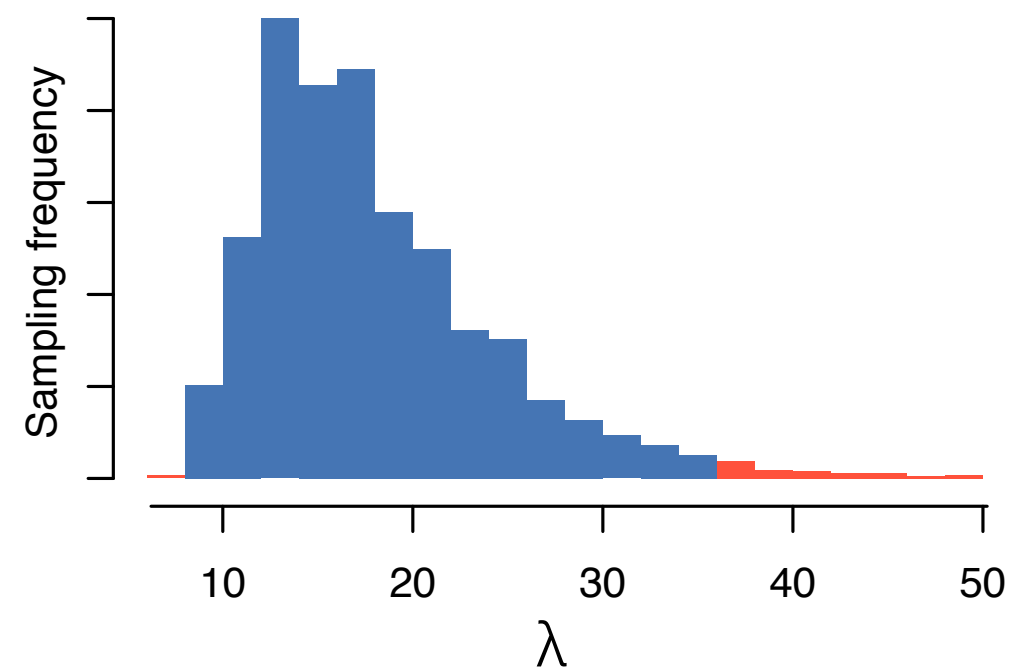
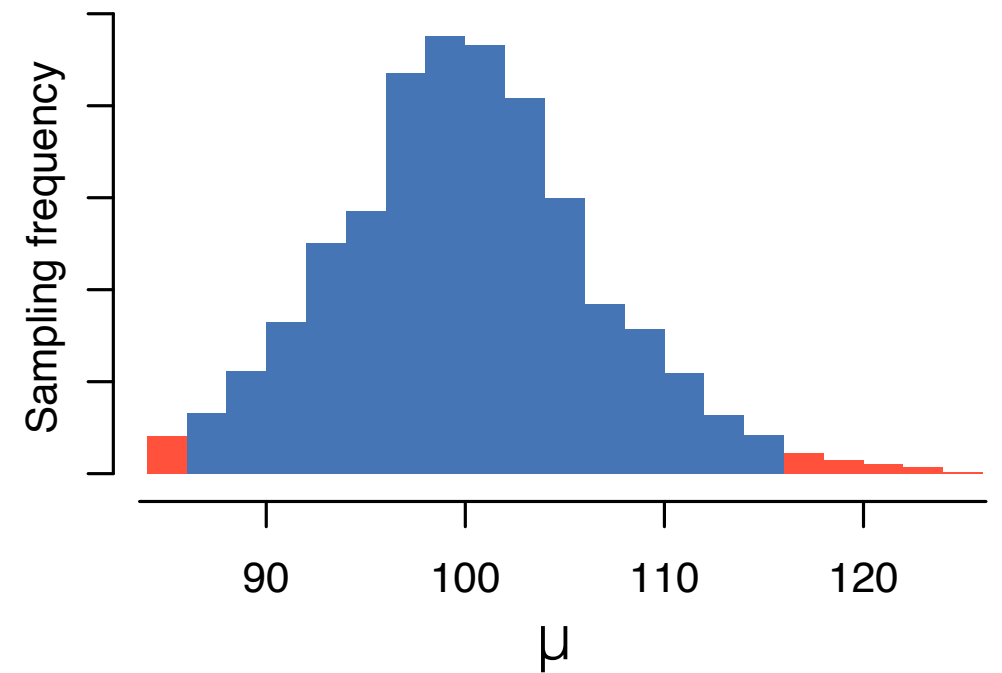
Summarizing MCMC samples



Summarizing MCMC samples

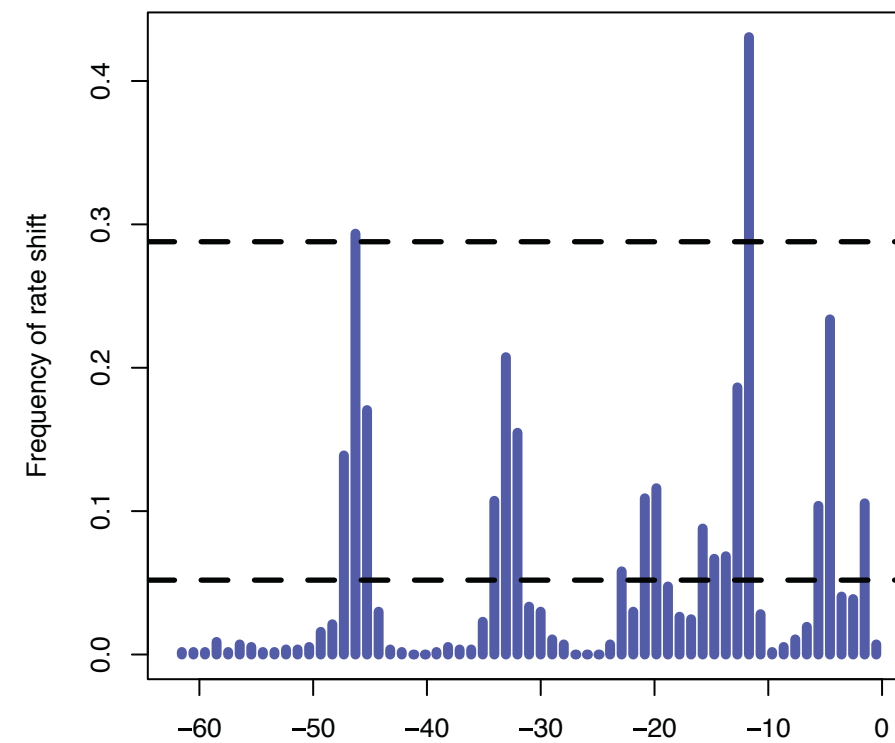
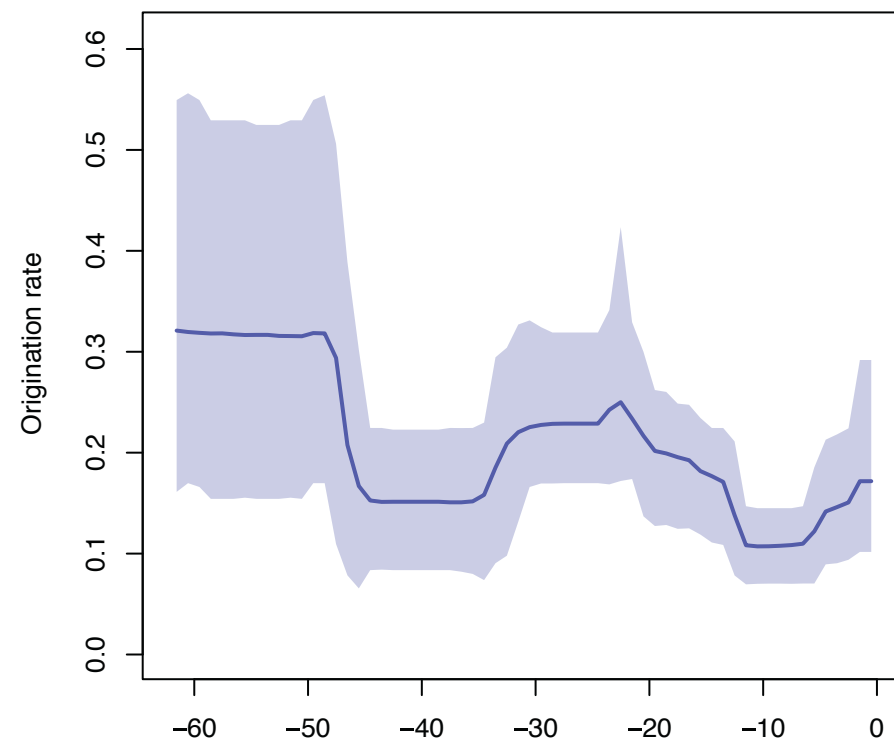
Posterior estimate: mean of
MCMC samples

95% Credible intervals



Plot results

```
PyRate — -zsh — 110x40
[mbp:~ $ cd Software/PyRate
[mbp:PyRate $ python PyRate.py -plotRJ your_path/pyrate_mcmc_logs -b 0.2]
```



Strong support for
a rate shift
($\log BF > 6$)

Significant rate shift
($\log BF > 2$)